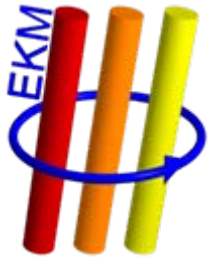


Dielectric properties of tissues and cells

Prof. Dr. Alois Loidl



Studies on the issue, if macroscopic dielectric properties of tissues have unlimited validity in both cellular and subcellular dimensions



Part of the German Mobile Telecommunication Research Programme

Participants:

- **Dielectric Spectroscopy** (A. Loidl, D. Egger, P. Lunkenheimer)
- Patch clamp measurements (A. Wixforth, M. Schneider)
- Theoretical calculations (P. Hänggi, G. Schmidt)

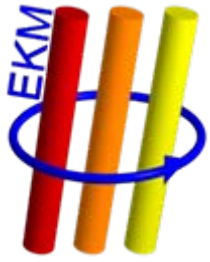
EKM / Institute of Physics, University of Augsburg, Germany



The project is financially supported by the Federal Office for Radiation Protection (BfS).



Bundesministerium
für Umwelt, Naturschutz
und Reaktorsicherheit



Studies on the issue, if macroscopic dielectric properties of tissues have unlimited validity in both cellular and subcellular dimensions



Introduction

Dielectric spectroscopy

Electrolytic solutions

Cell suspensions

Summary

Behaviour of dielectric parameters at cellular and subcellular dimensions

- Permittivity ε and conductivity σ are determining factors in absorption of electromagnetic radiation
- dosimetry essentially relies on the knowledge of dielectric properties of tissue

Specific Absorption Rate

$$SAR = \frac{\sigma |E|^2}{\rho}$$

σ : conductivity (S/m)

E : field strength (V/m)

ρ : mass density (kg/m³)

Studies on the issue, if macroscopic dielectric properties of tissues have unlimited validity in both cellular and subcellular dimensions

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Dielectric spectroscopy

complex permittivity: $\epsilon^* = \epsilon' - i \epsilon''$ complex conductivity: $\sigma^* = \sigma' + i \sigma''$

dielectric constant ϵ' dielectric loss ϵ''

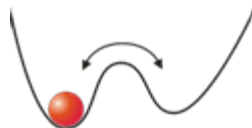
$$\sigma^* = i \omega \epsilon_0 \epsilon^*$$

relaxation

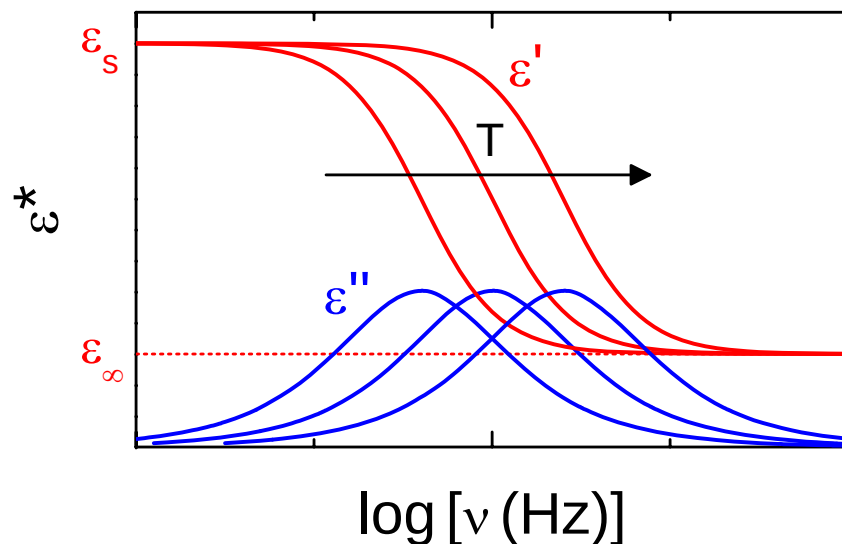
reorienting
dipolar
molecule



charged
particle in
double-well
potential



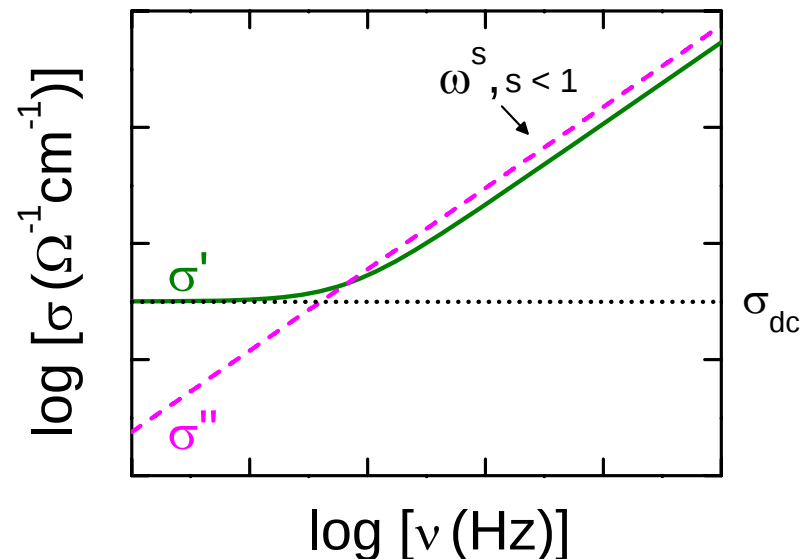
peak in $\epsilon''(\nu, T)$, step in $\epsilon'(\nu, T)$ at $\nu = 1/(2\pi\tau)$



hopping conduction



$$\sigma' = \sigma_{dc} + \sigma_0 \nu^s \quad (s < 1)$$



Dielectric spectroscopy

$$\varepsilon^*(\omega) = \varepsilon_\infty + \frac{\varepsilon_s - \varepsilon_\infty}{[1 + (i\omega\tau)^{1-\alpha}]^\beta} - i \frac{\sigma_{dc}}{\varepsilon_0 \omega}$$

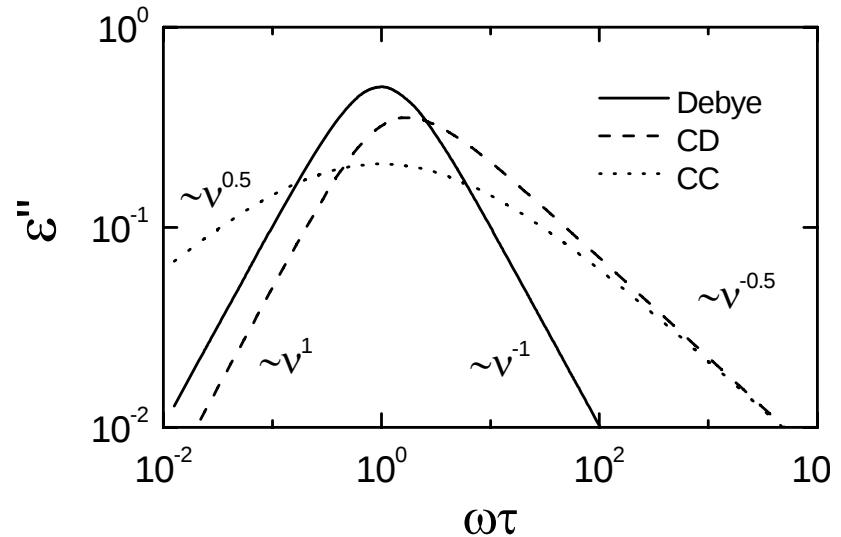
$$\tau = \tau_0 \cdot \exp\left(\frac{E_\tau}{k_B(T - T_{VF})}\right)$$

or

$$\tau = \frac{1}{2D_R}$$

Rotational diffusion coefficient

$$D_R = \frac{k_B T}{8\pi\eta r_H^3} \quad \begin{array}{l} \eta \text{ viscosity} \\ r_H \text{ hydrodyn. radius} \end{array}$$



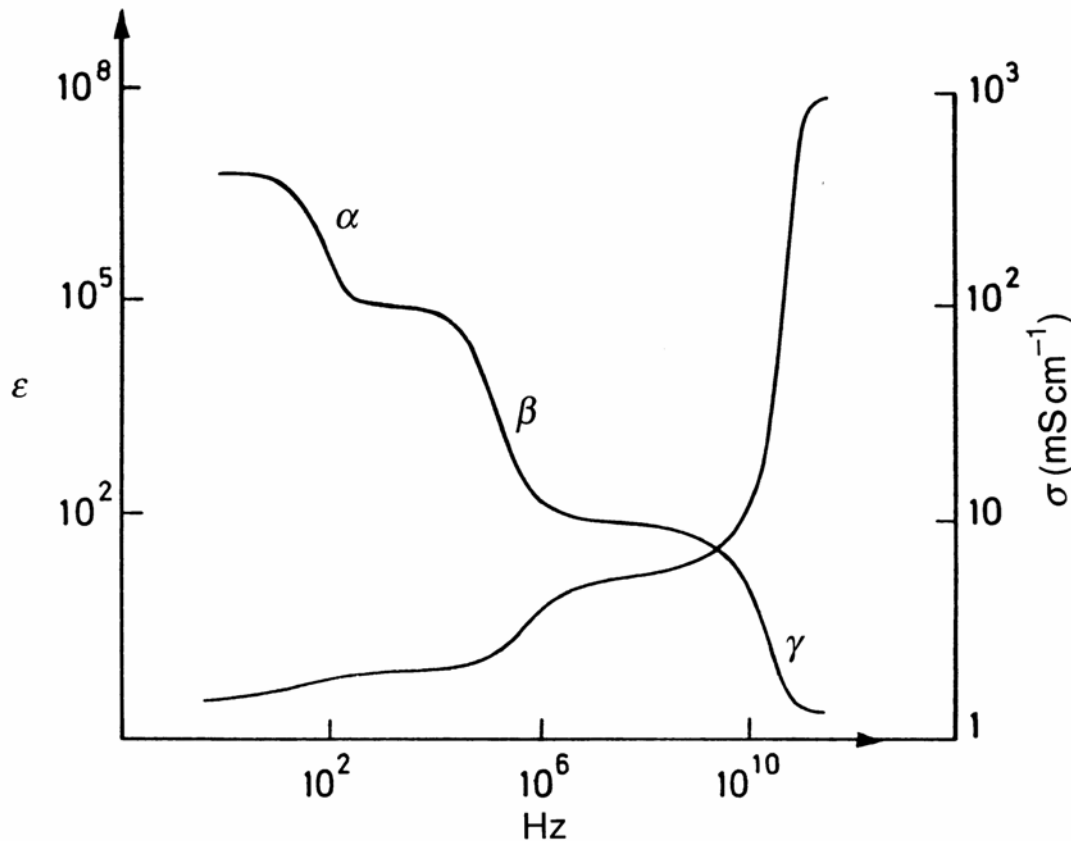
$$\sigma_{dc} = \sigma_0 \cdot \exp\left(-\frac{E_\sigma}{k_B T}\right)$$

$$\sigma_0 = \frac{n_0 q^2 a^2 \nu_0}{6k_B T}$$

$$D_\sigma = \frac{k_B T \sigma_{dc}}{(ne)^2} \quad \begin{array}{l} \text{Conductivity} \\ \text{diffusion} \\ \text{(Nernst-Einstein)} \end{array}$$

Dielectric spectroscopy

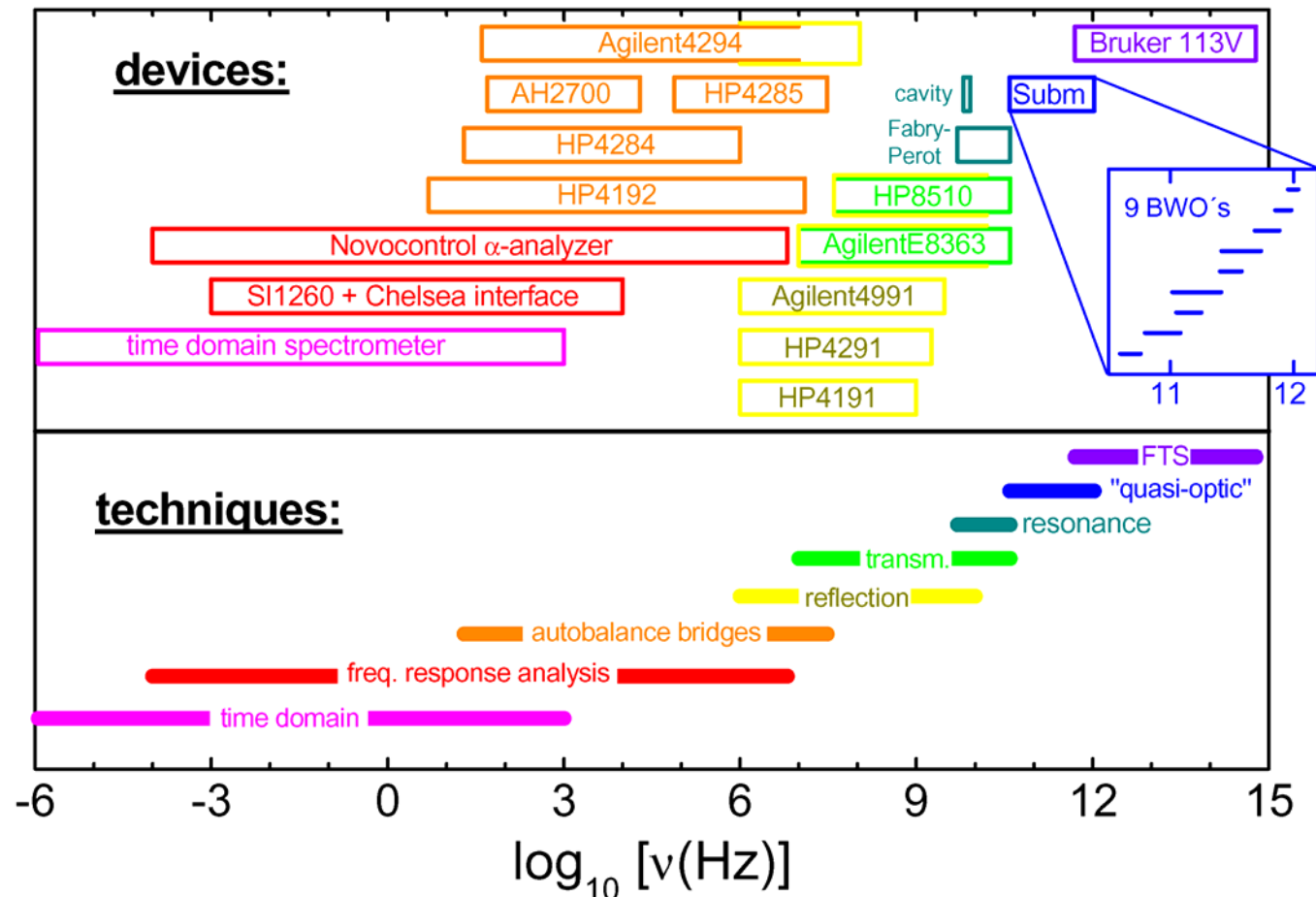
Major dispersion regimes in biological matter



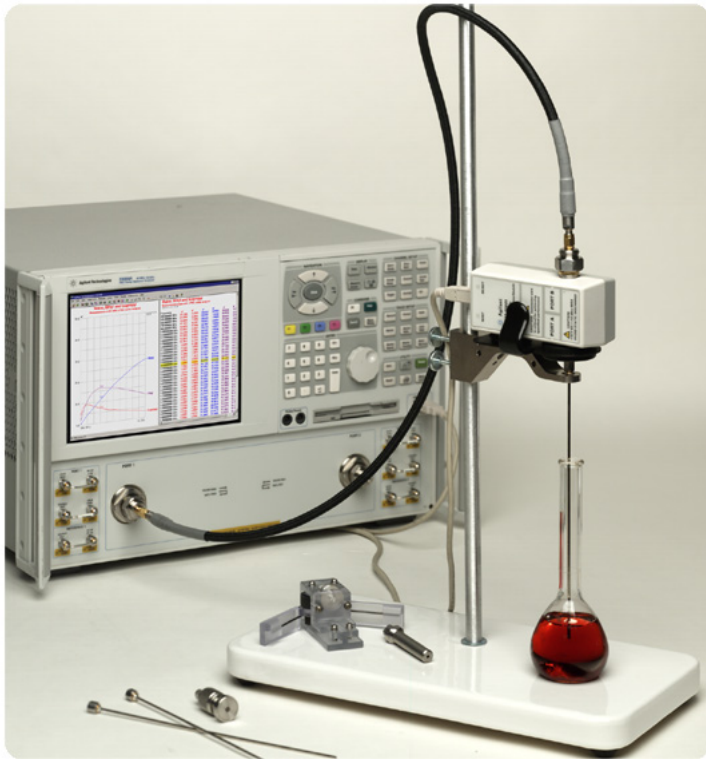
- **α -dispersion**
counter-ion relaxation?
membrane structure/channels?
- **β -dispersion**
1 kHz...100 MHz
charging of cell membranes
- **γ -dispersion**
> 100 MHz
rotation of water molecule
- **δ -dispersion**
bound water
relaxation of macromolecules

Broadband dielectric spectroscopy

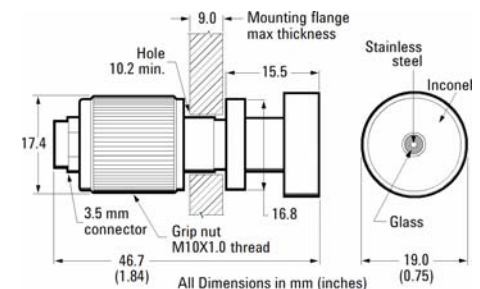
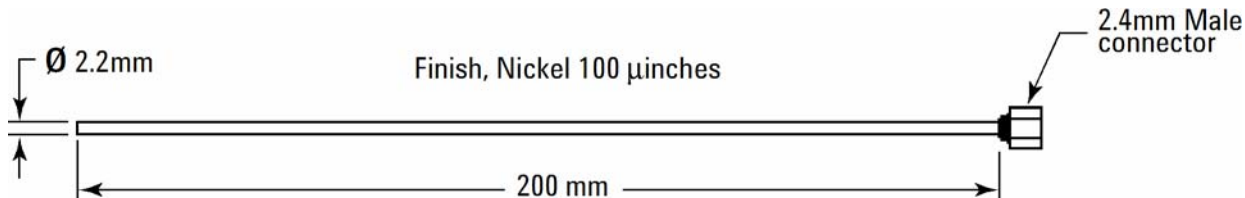
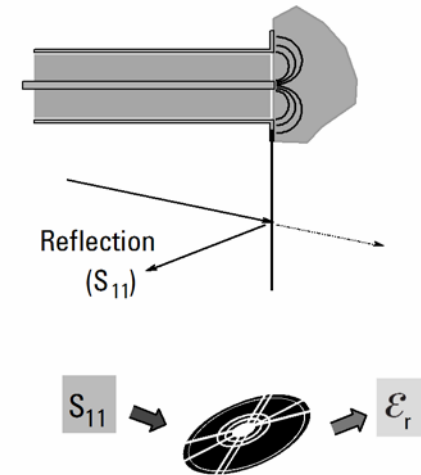
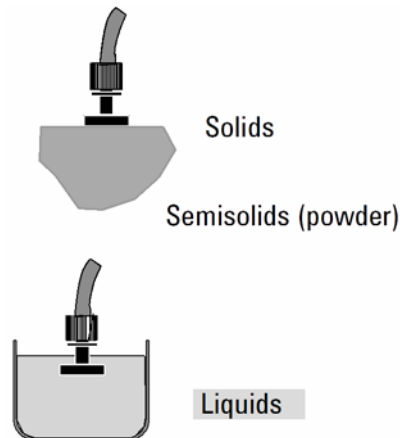
- Measurement of dielectric constant and complex conductivity
- Parameters: frequency, temperature ($0.1 \text{ K} < T < 1000 \text{ K}$), doping, magnetic field
- Extremely **broad frequency range**: $10^{-6} \text{ Hz} < \nu < 10^{15} \text{ Hz}$



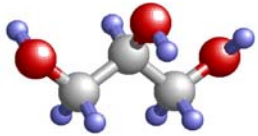
Open-ended coaxial probe (100 MHz - 40 GHz)



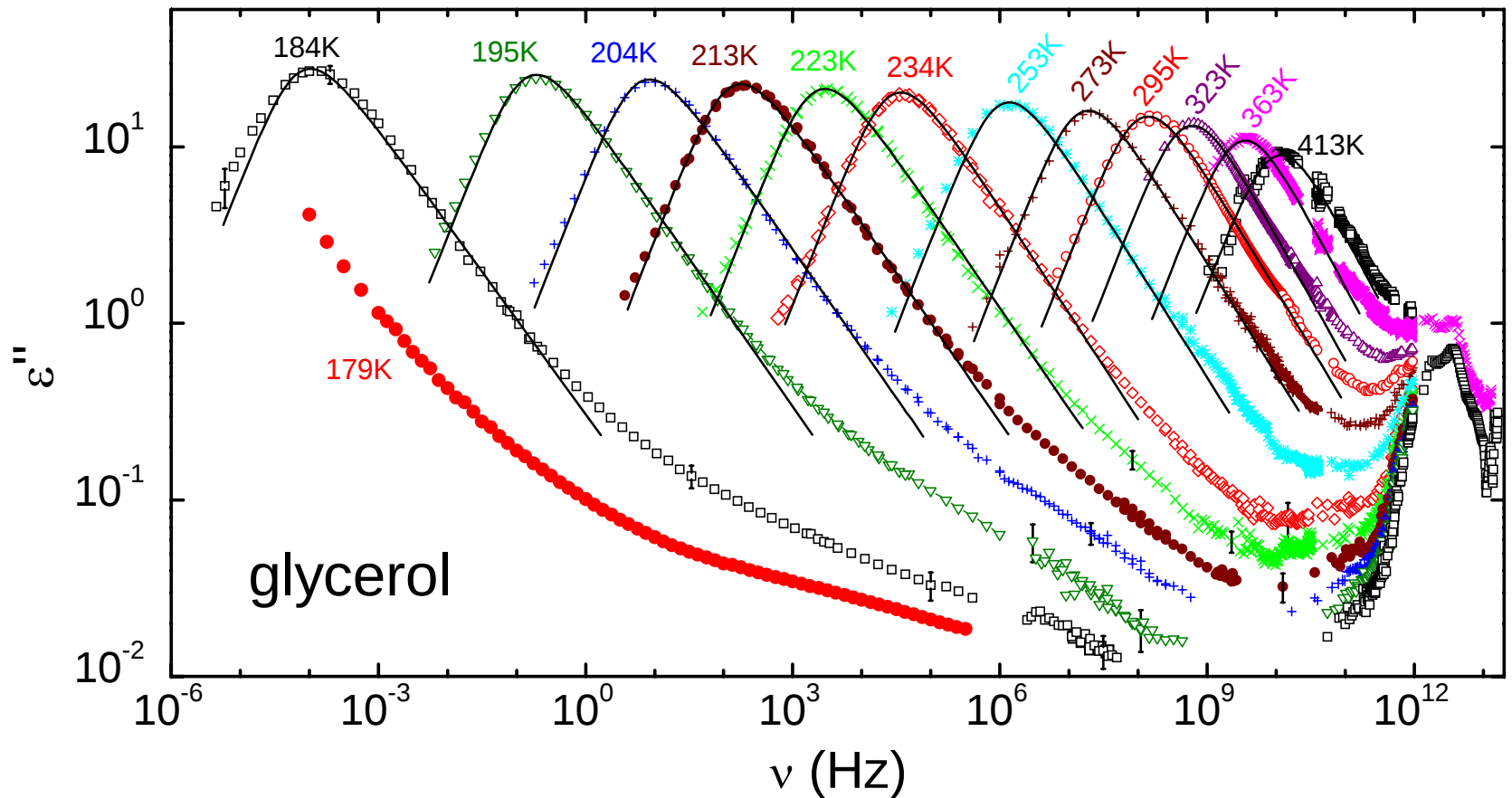
- Ideal for liquids or semisolids
- measurements with network analyzer (Agilent E8363B PNA Series)



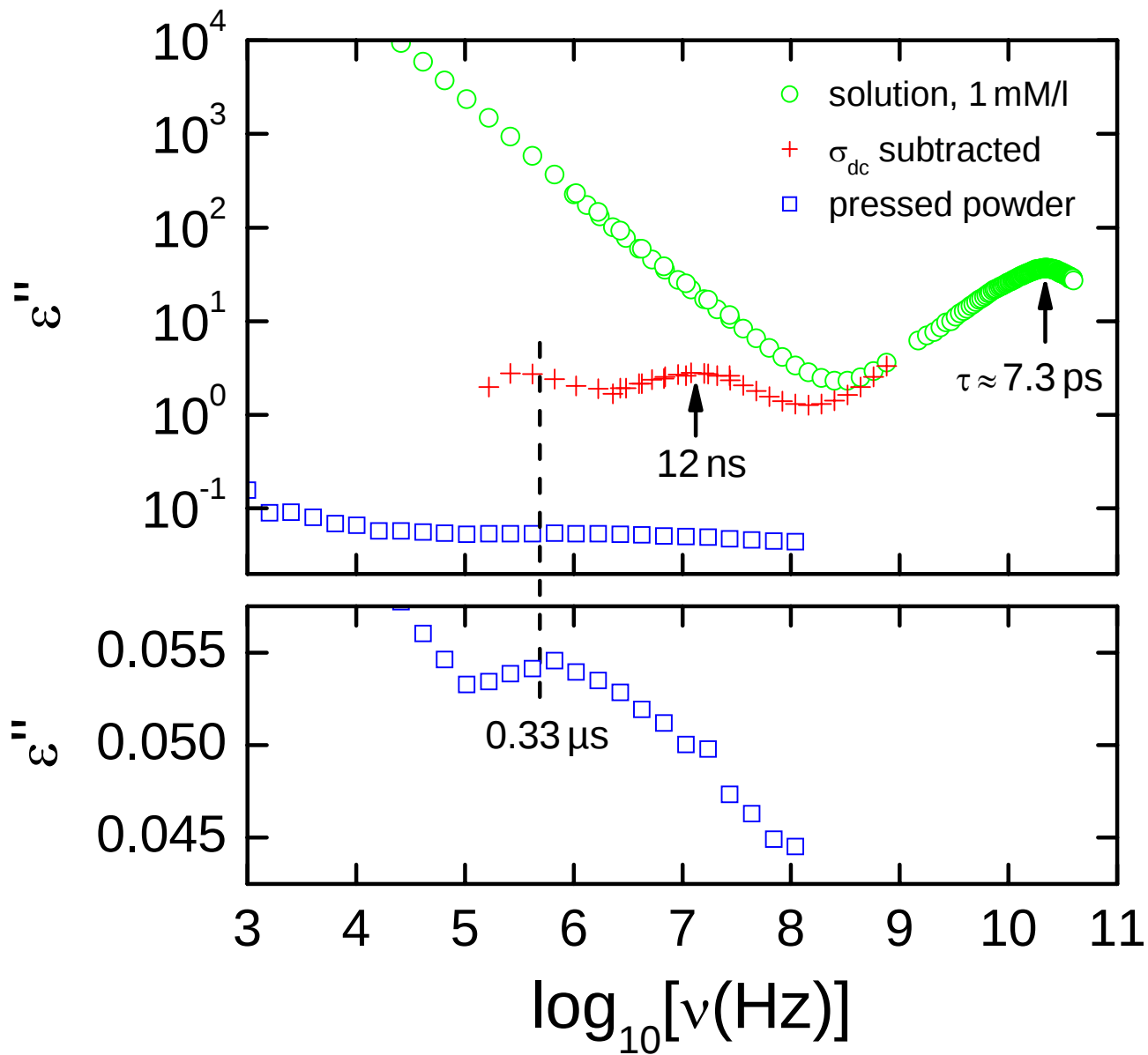
Example: glycerol



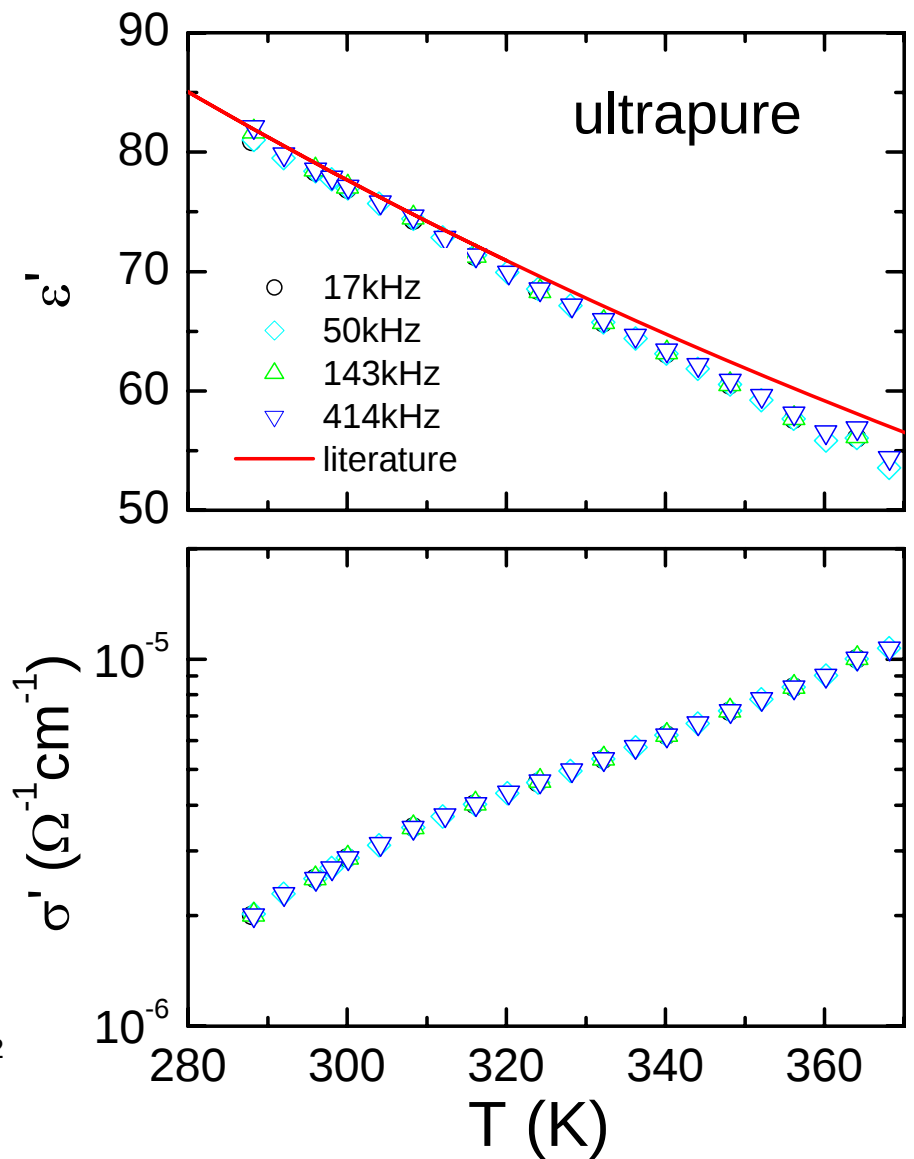
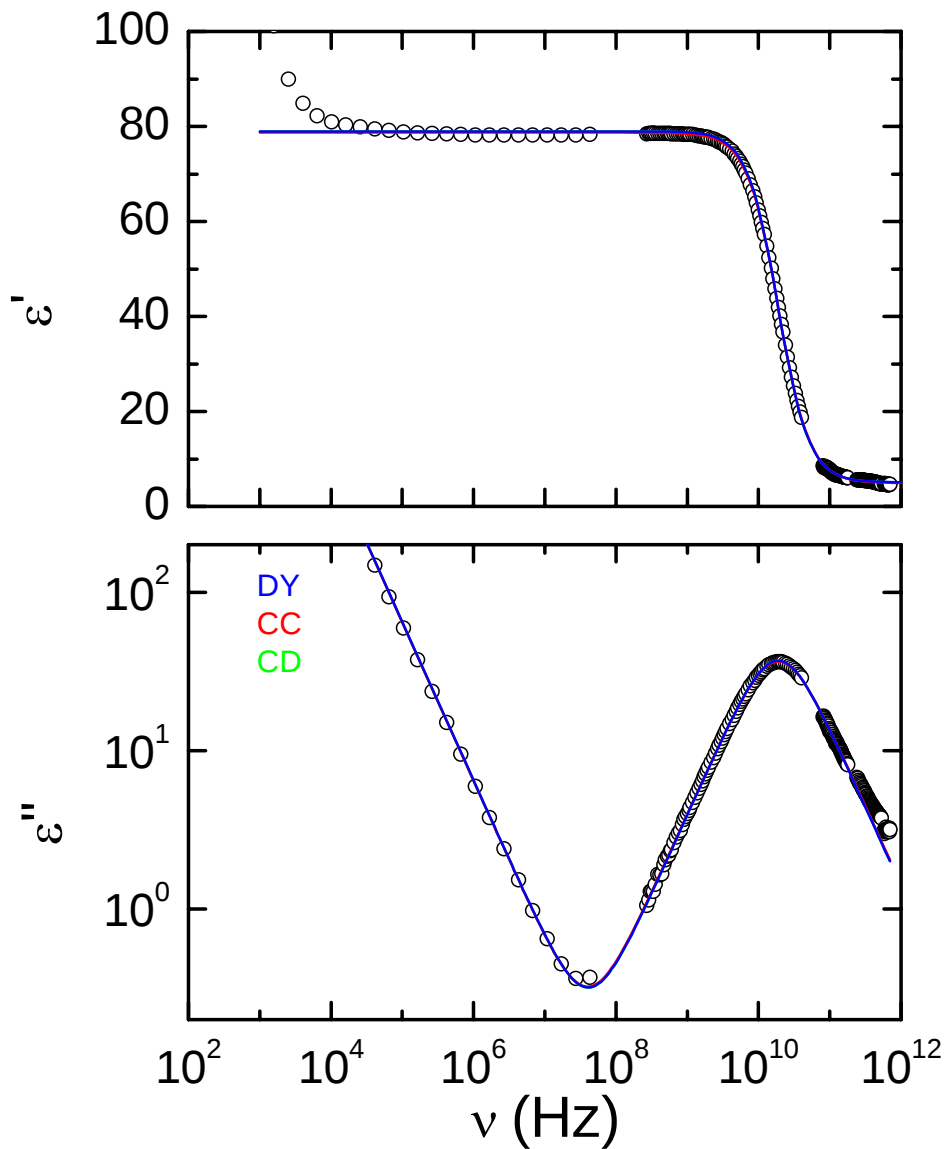
$\text{C}_3\text{H}_8\text{O}_3$
network glass former (hydrogen bonded)
 $T_m=291\text{ K}$; $T_g\approx 185\text{ K}$



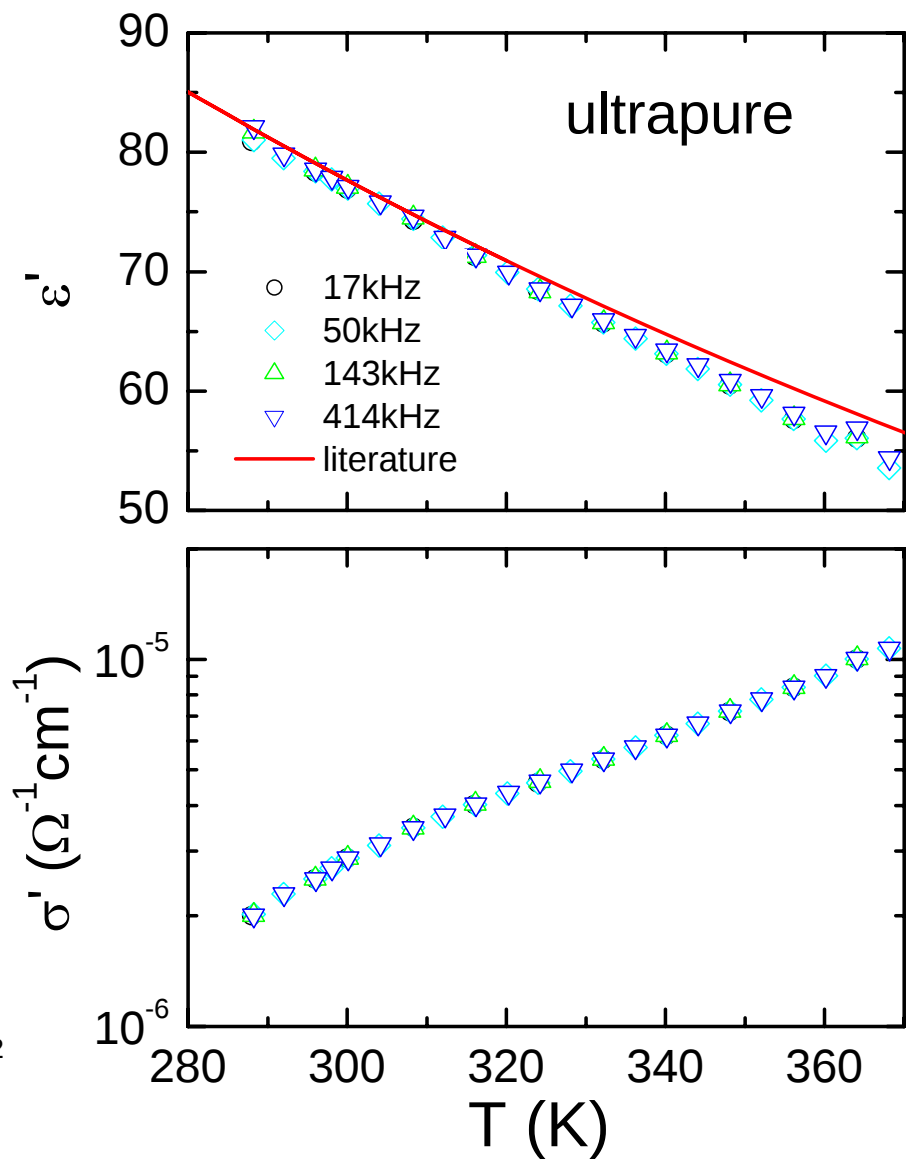
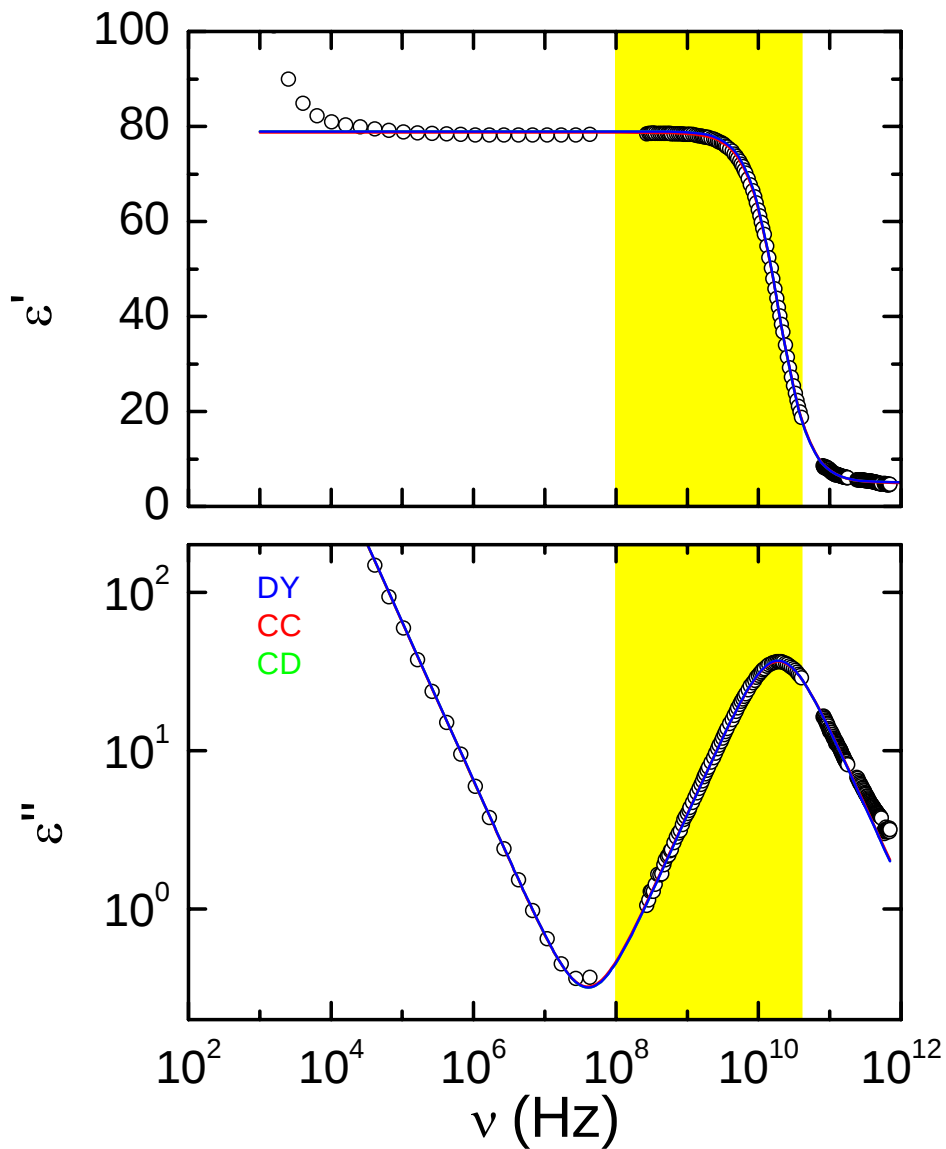
Ubiquitin



Dielectric properties of pure water



Dielectric properties of pure water



Studies on the issue, if macroscopic dielectric properties of tissues have unlimited validity in both cellular and subcellular dimensions

Introduction

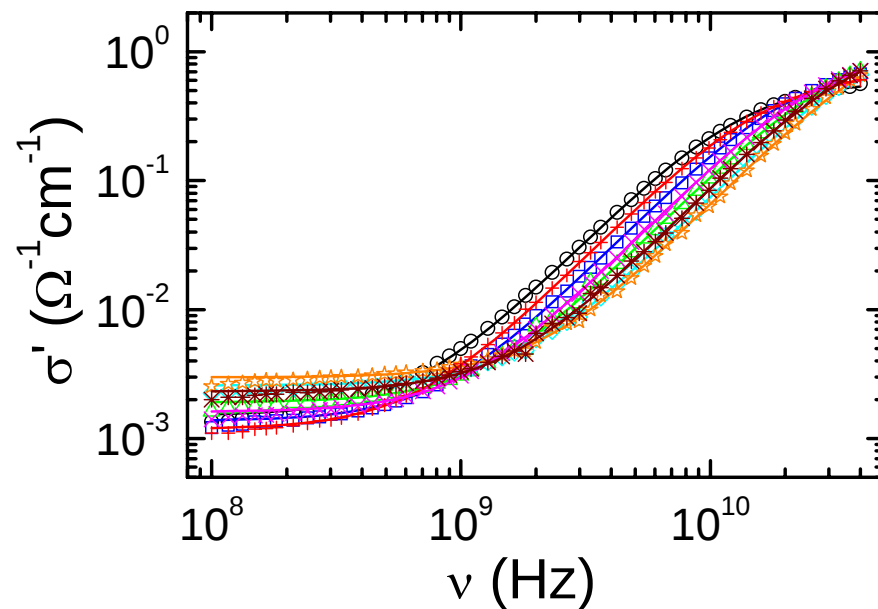
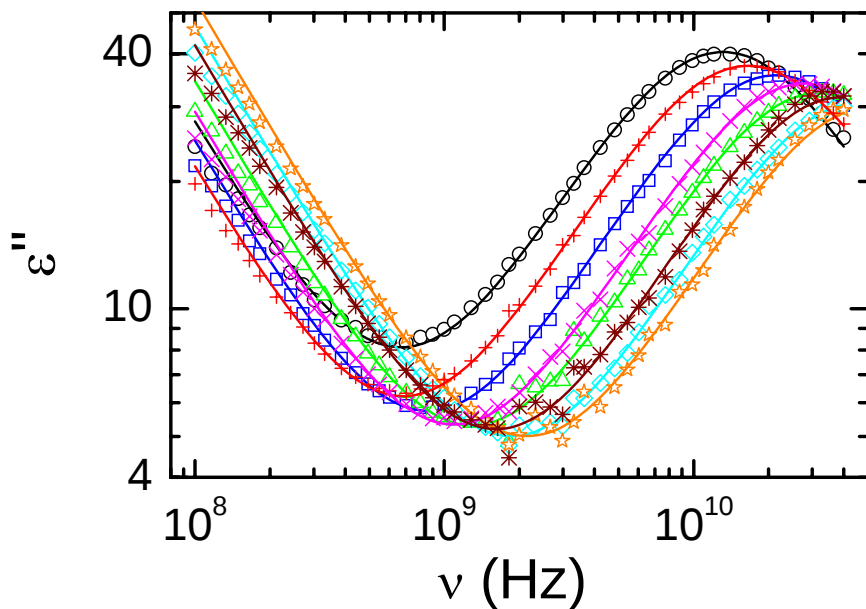
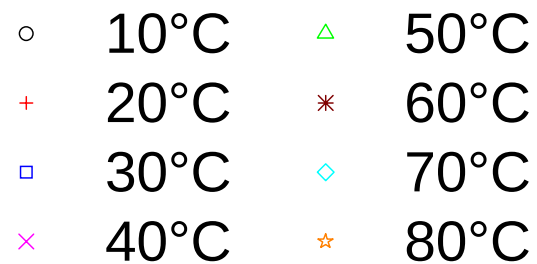
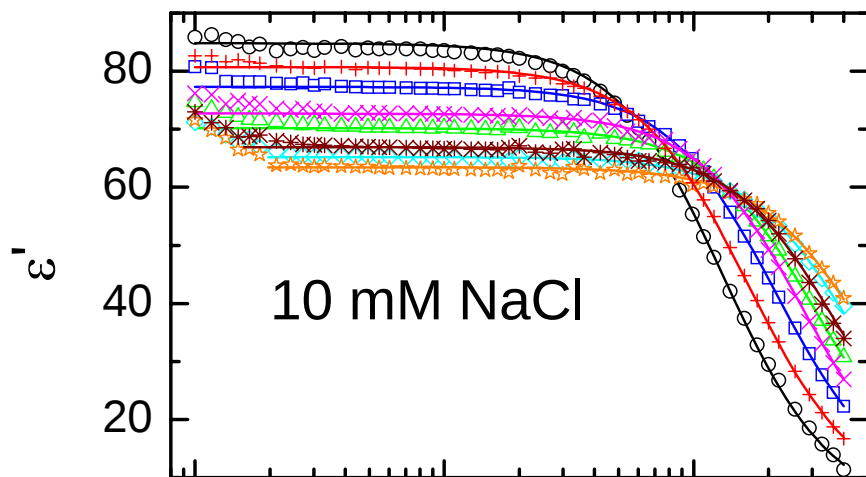
Dielectric spectroscopy

Electrolytic solutions

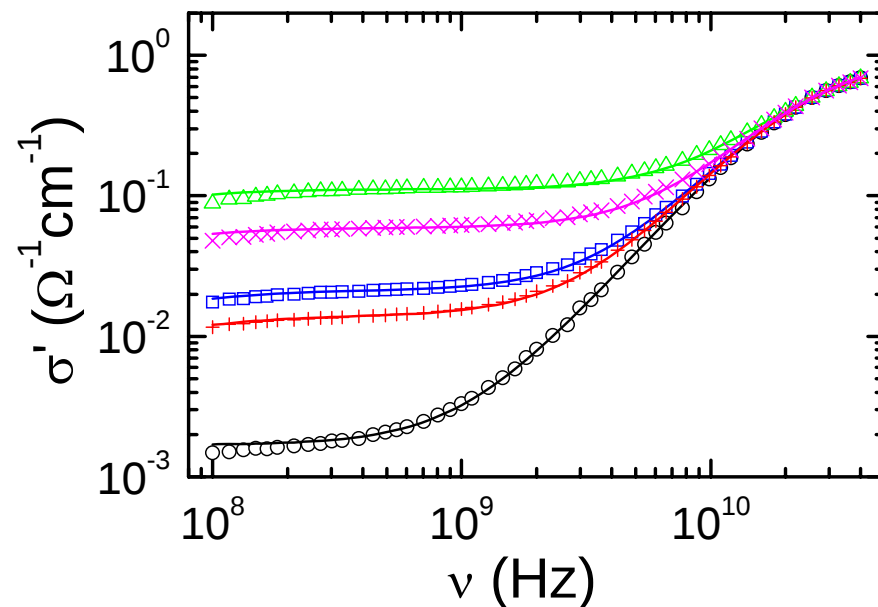
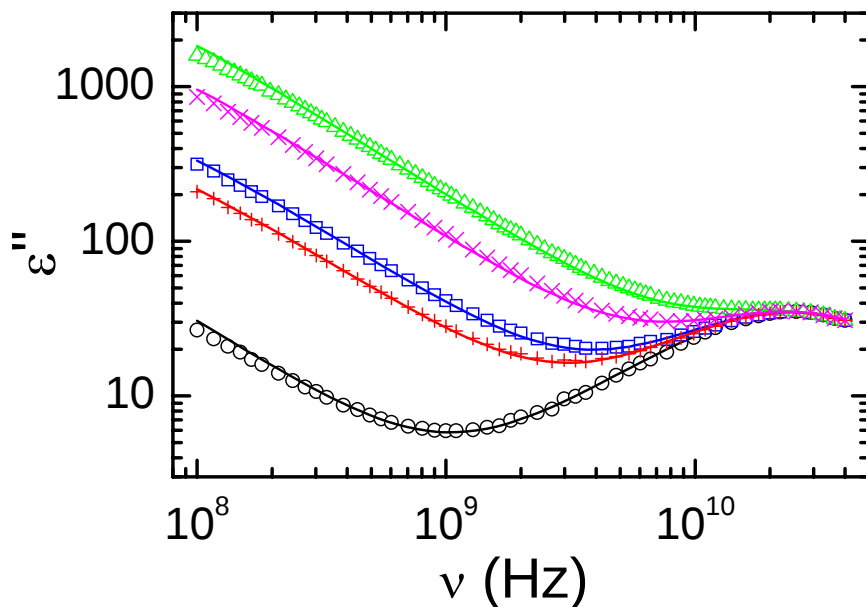
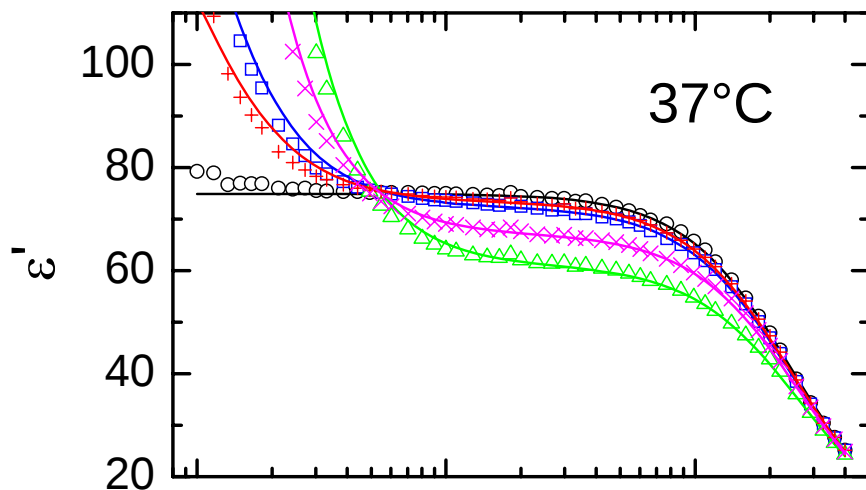
Cell suspensions

Summary

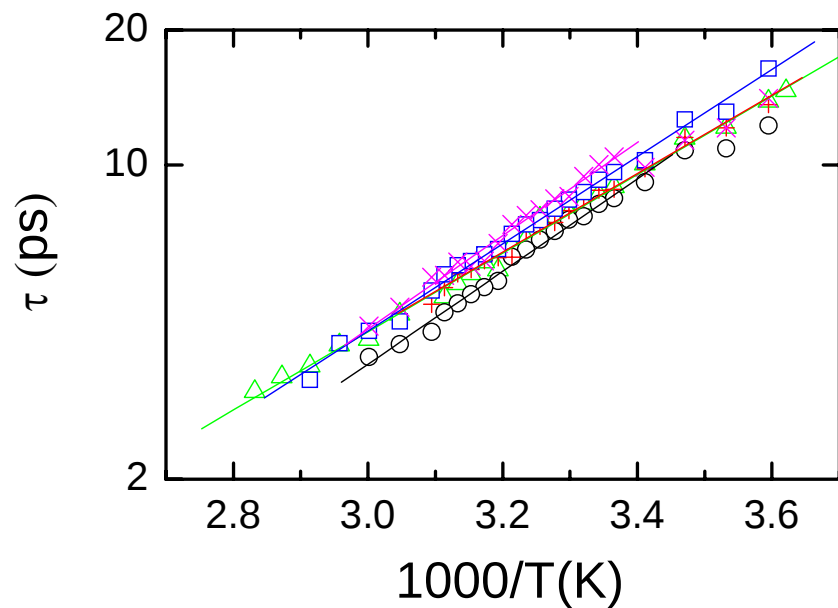
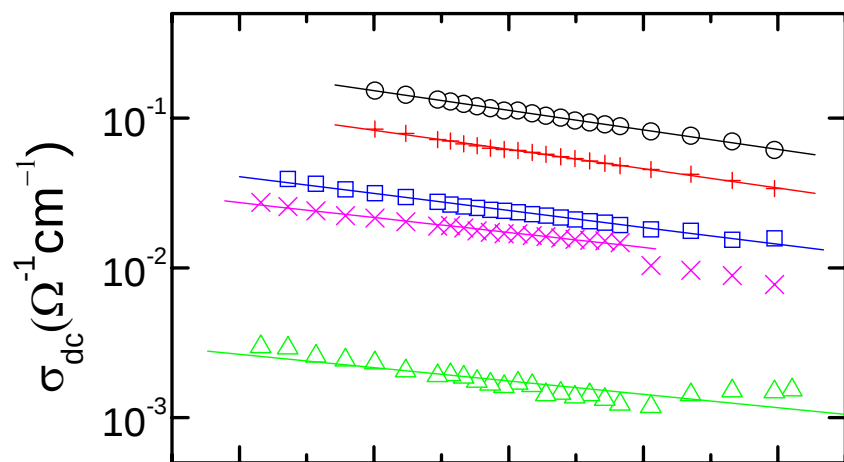
Electrolytic solutions



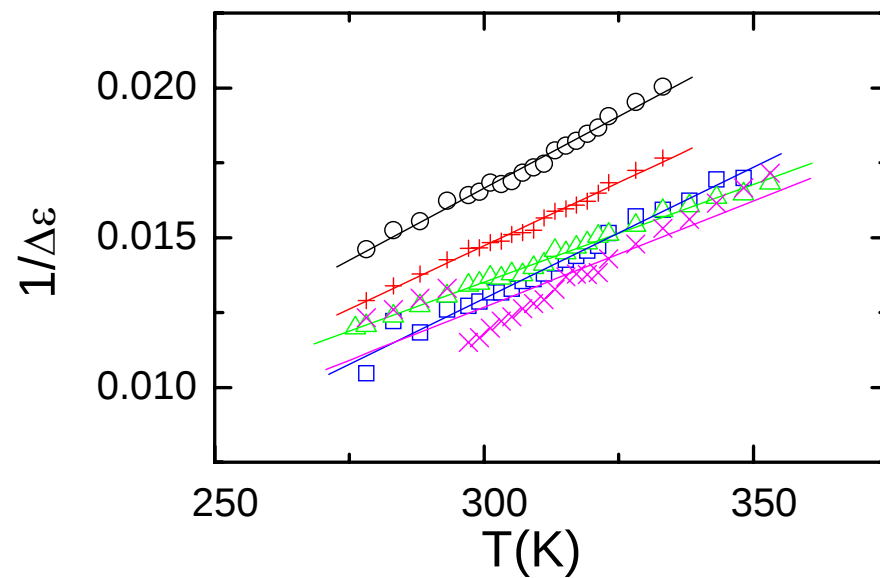
Electrolytic solutions



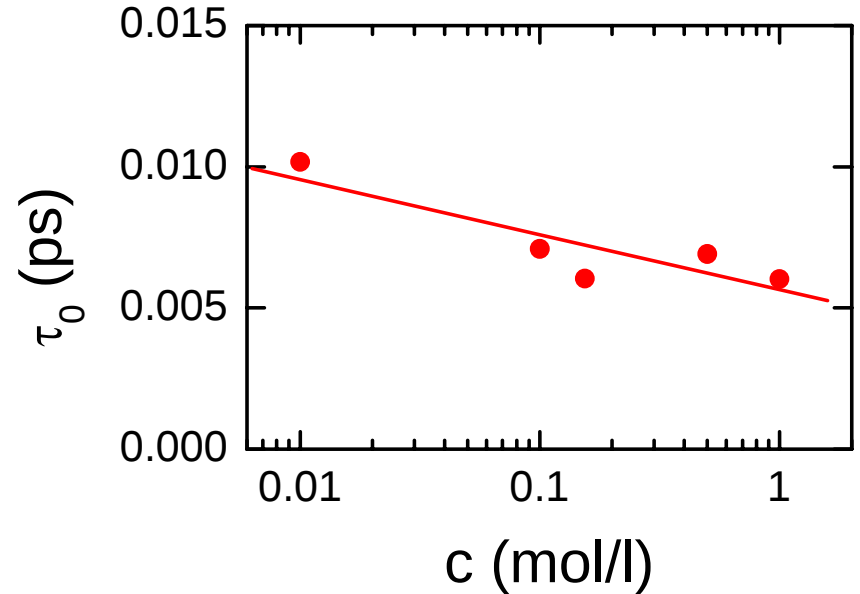
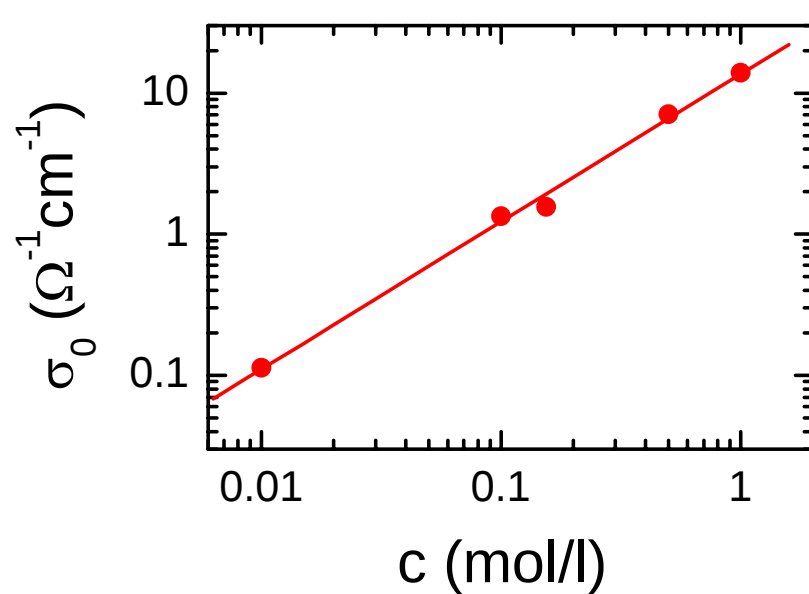
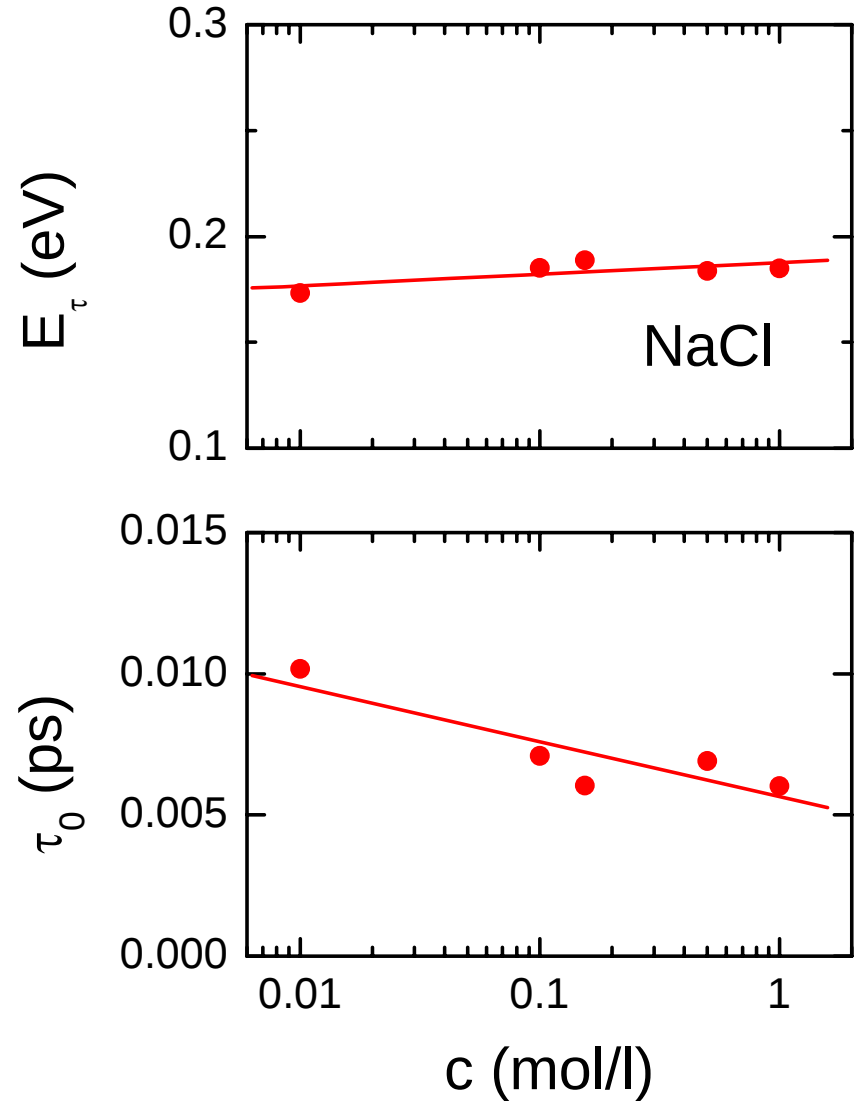
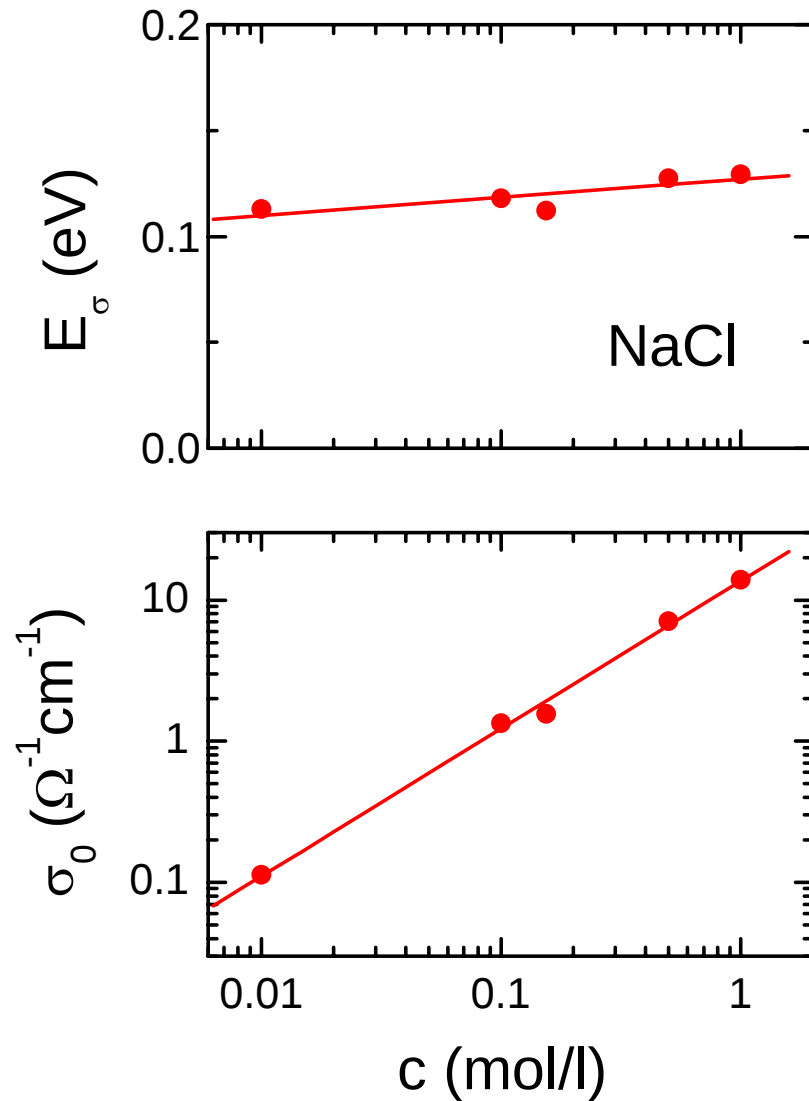
Fitparameters: NaCl electrolytes



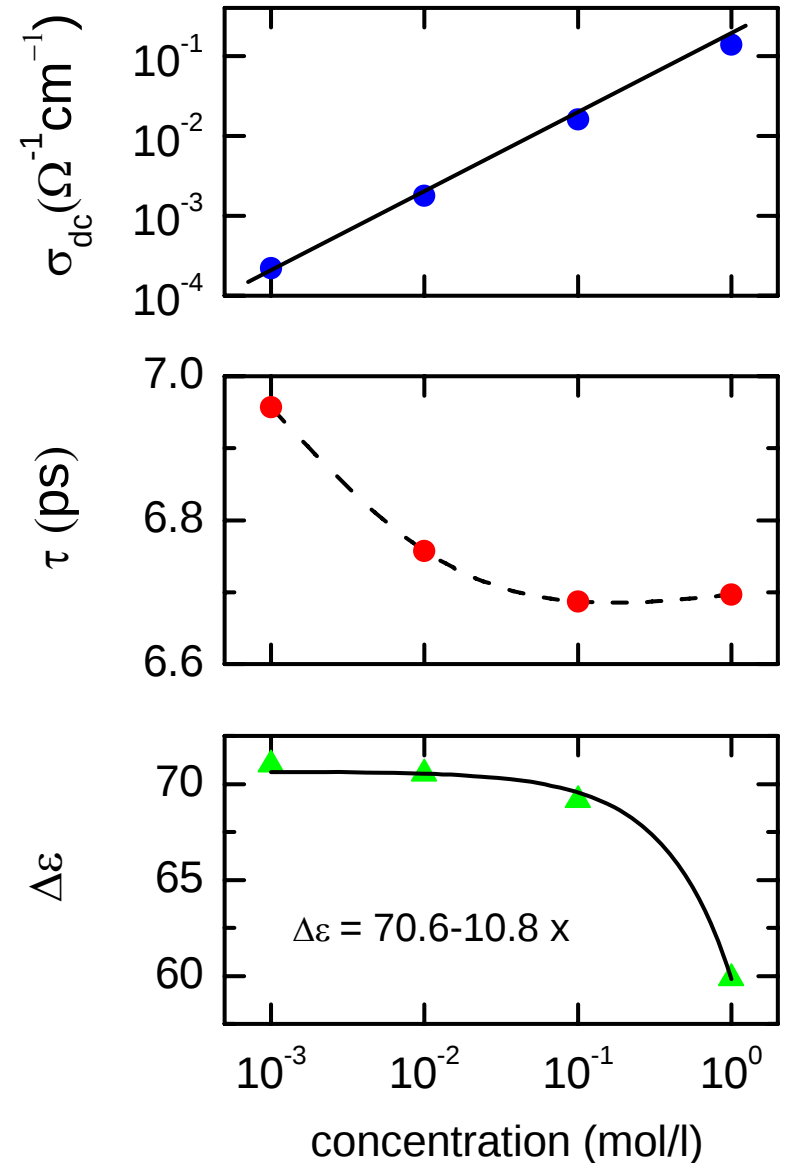
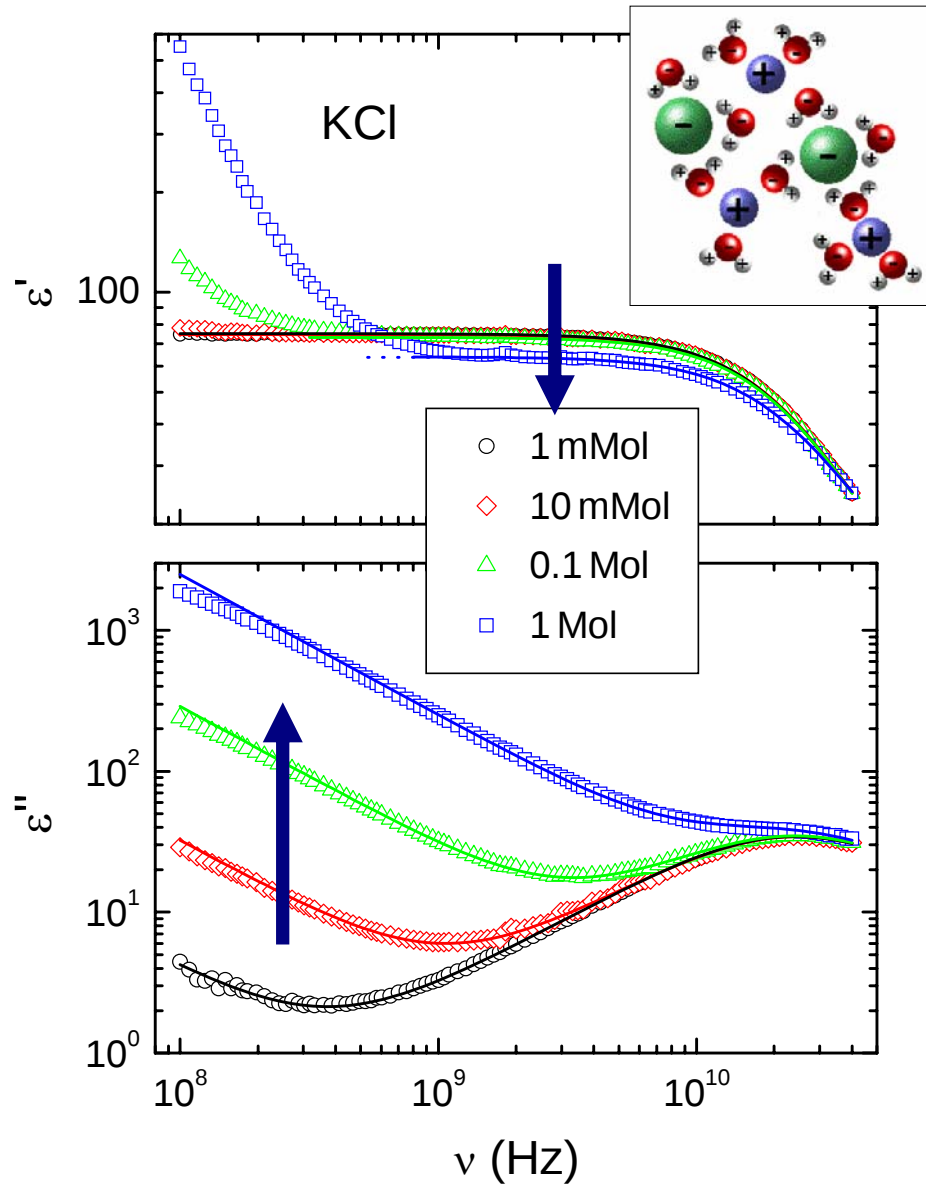
- 1 M NaCl
- + 0.5 M NaCl
- 0.154 M NaCl
- × 0.100 M NaCl
- △ 0.010 M NaCl



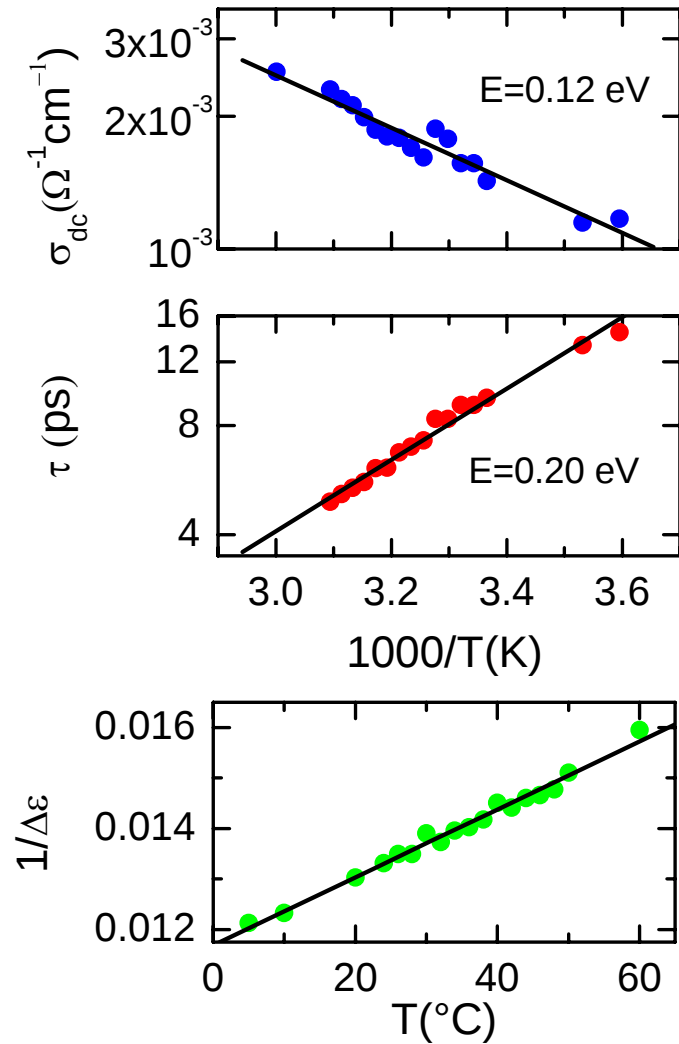
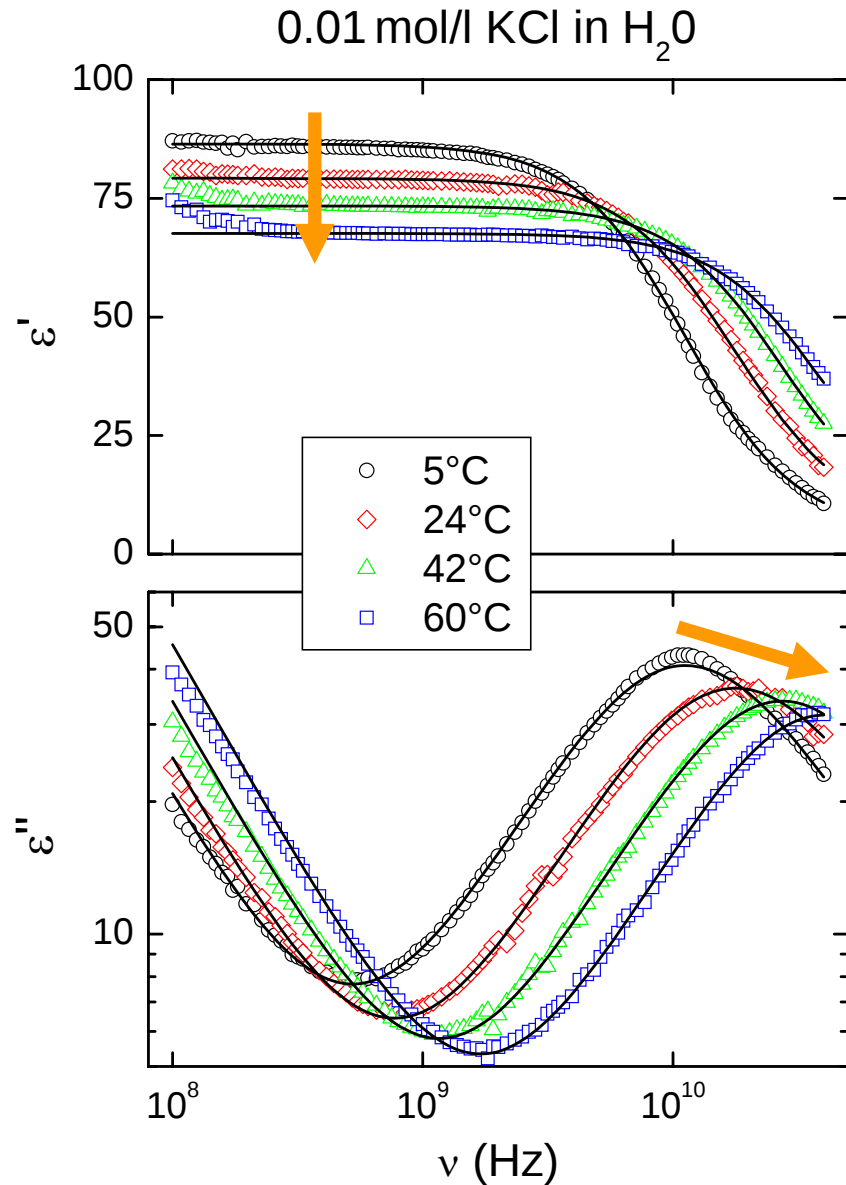
Hindering barriers and prefactors of electrolytic solutions



Electrolytic solutions (concentration dependence)

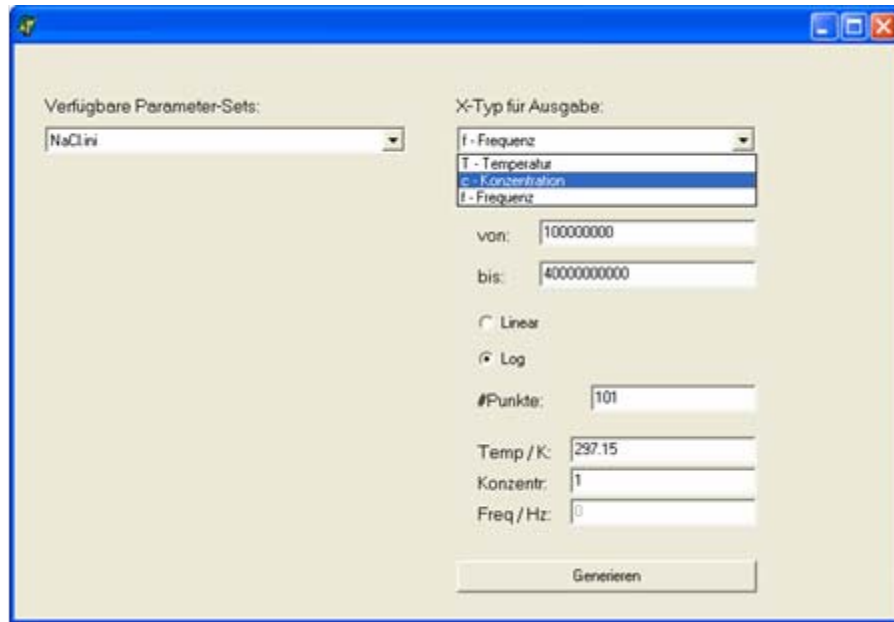


Electrolytic solutions (temperature dependence)



Universal description of electrolytic solutions

$$\varepsilon^*(\omega) = \varepsilon_\infty + \frac{\varepsilon_s - \varepsilon_\infty}{\left[1 + (i\omega\tau)^{1-\alpha}\right]^\beta} - i \frac{\sigma_{dc}}{\varepsilon_0 \omega}$$



$$\Delta\varepsilon = \varepsilon_s - \varepsilon_\infty = \frac{C}{T - T_c}$$

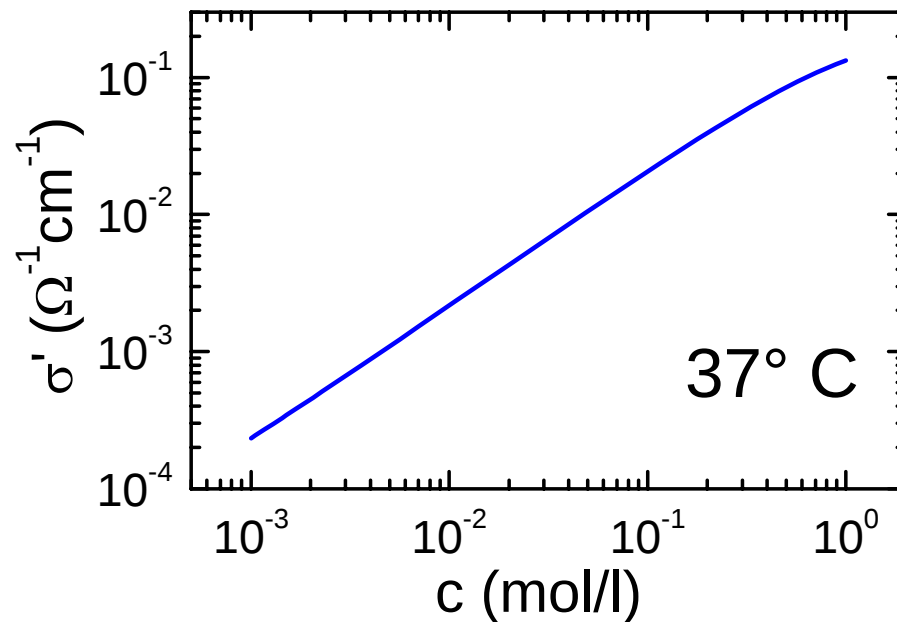
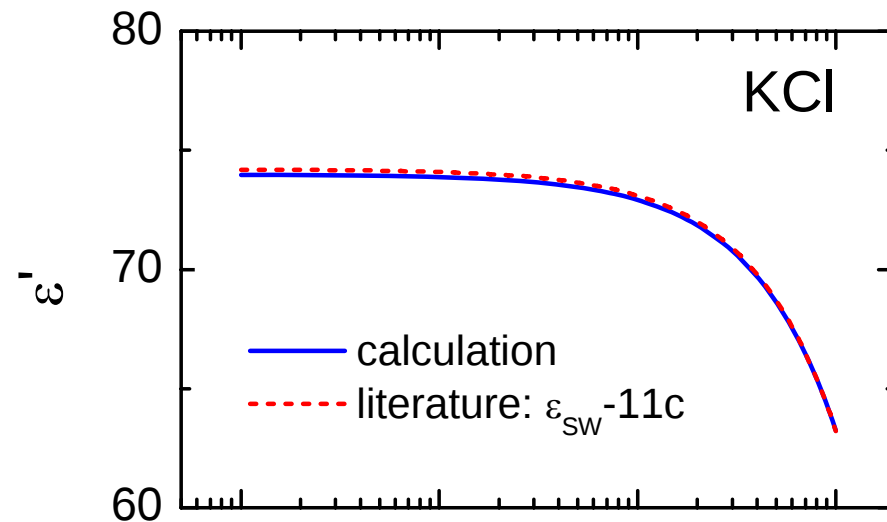
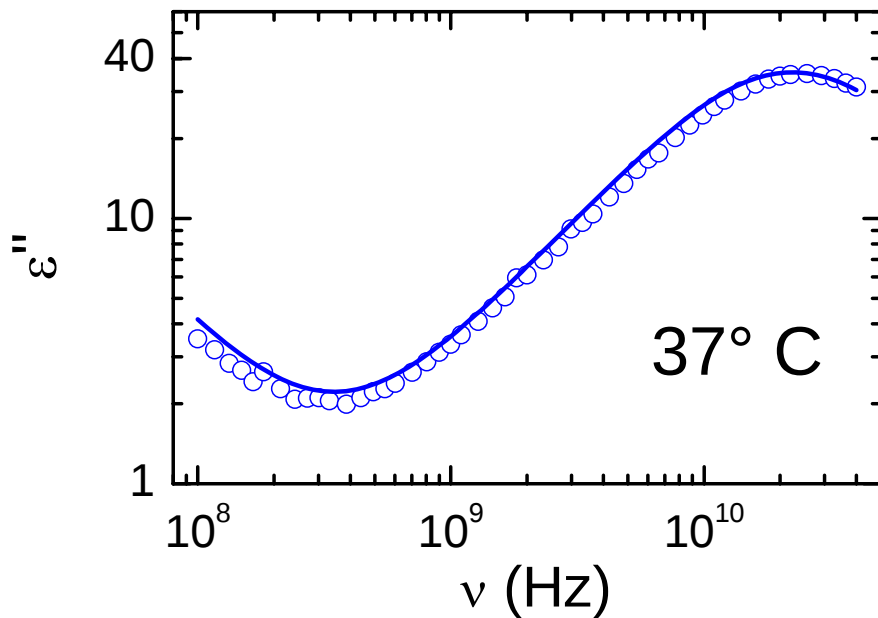
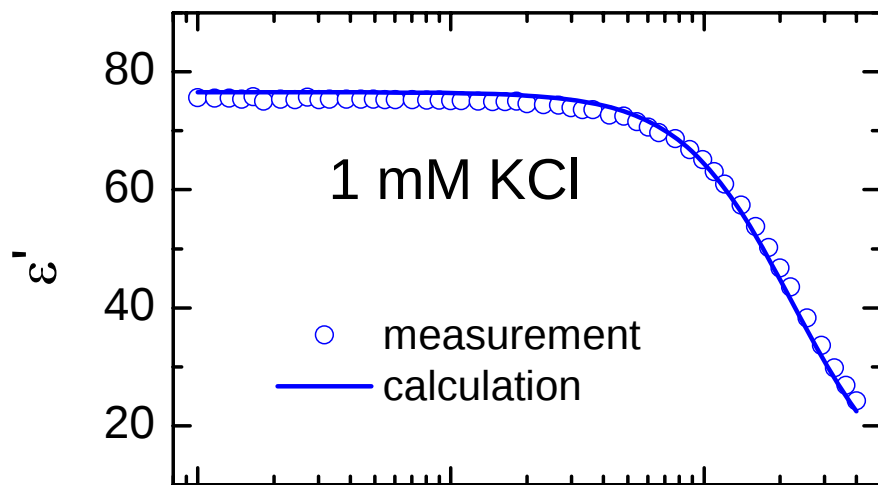
$$\tau = \tau_0 \cdot \exp\left(\frac{E_\tau}{k_B T}\right)$$

$$\sigma_{dc} = \sigma_0 \cdot \exp\left(-\frac{E_\sigma}{k_B T}\right)$$

Max. 14 Parameter:

ε_∞ , α , β , A_{curie} , B_{curie} , AT_{curie} , BT_{curie} ,
 $A\sigma_0$, AE_σ , BE_σ , $A\tau_0$, $B\tau_0$, AE_τ , BE_τ ,

ε and σ as function of ν , c , T



Studies on the issue, if macroscopic dielectric properties of tissues have unlimited validity in both cellular and subcellular dimensions

Introduction

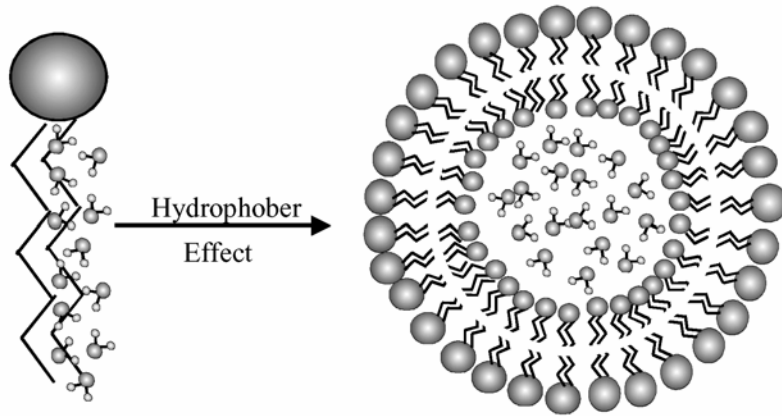
Dielectric spectroscopy

Electrolytic solutions

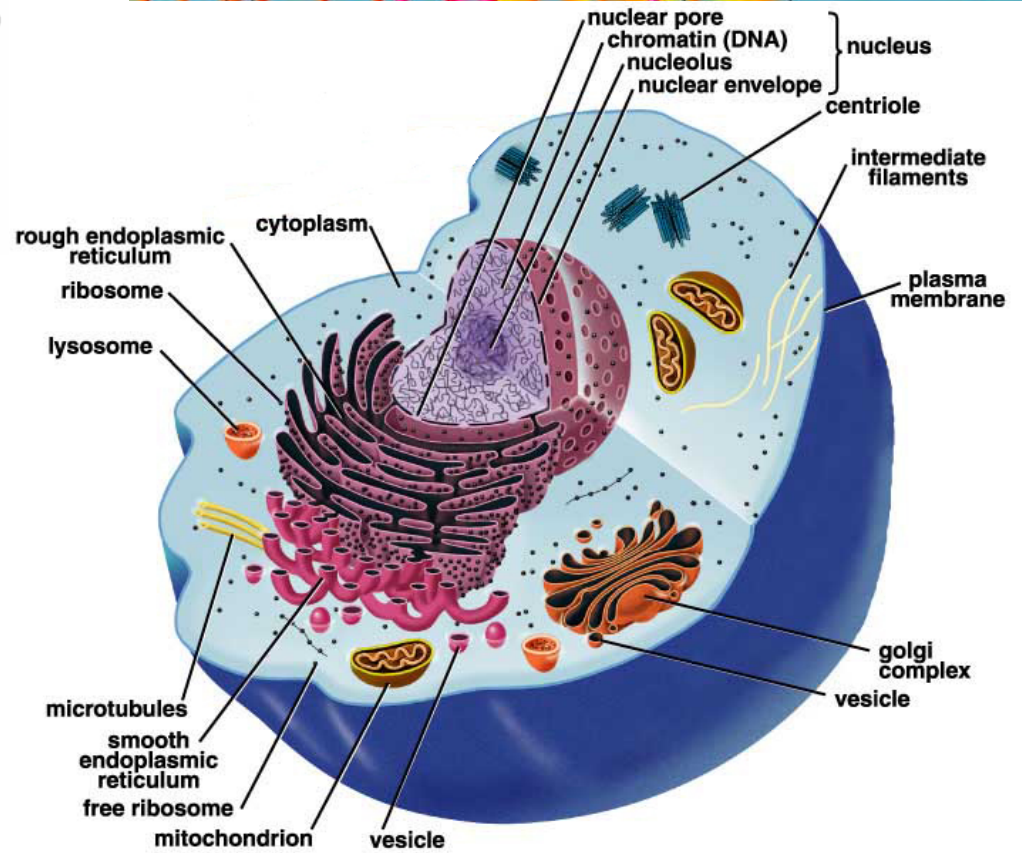
Cell suspensions

Summary

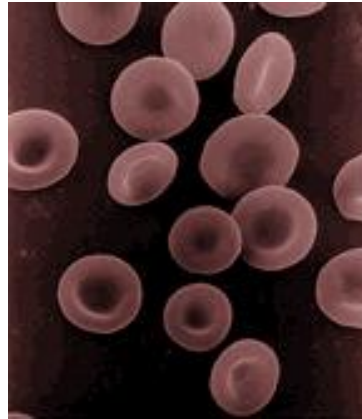
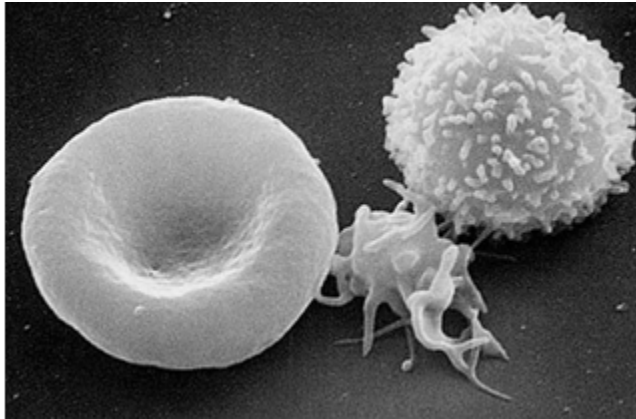
Dielectric properties of cell suspensions



Unilamellar vesicles as
cellular model systems



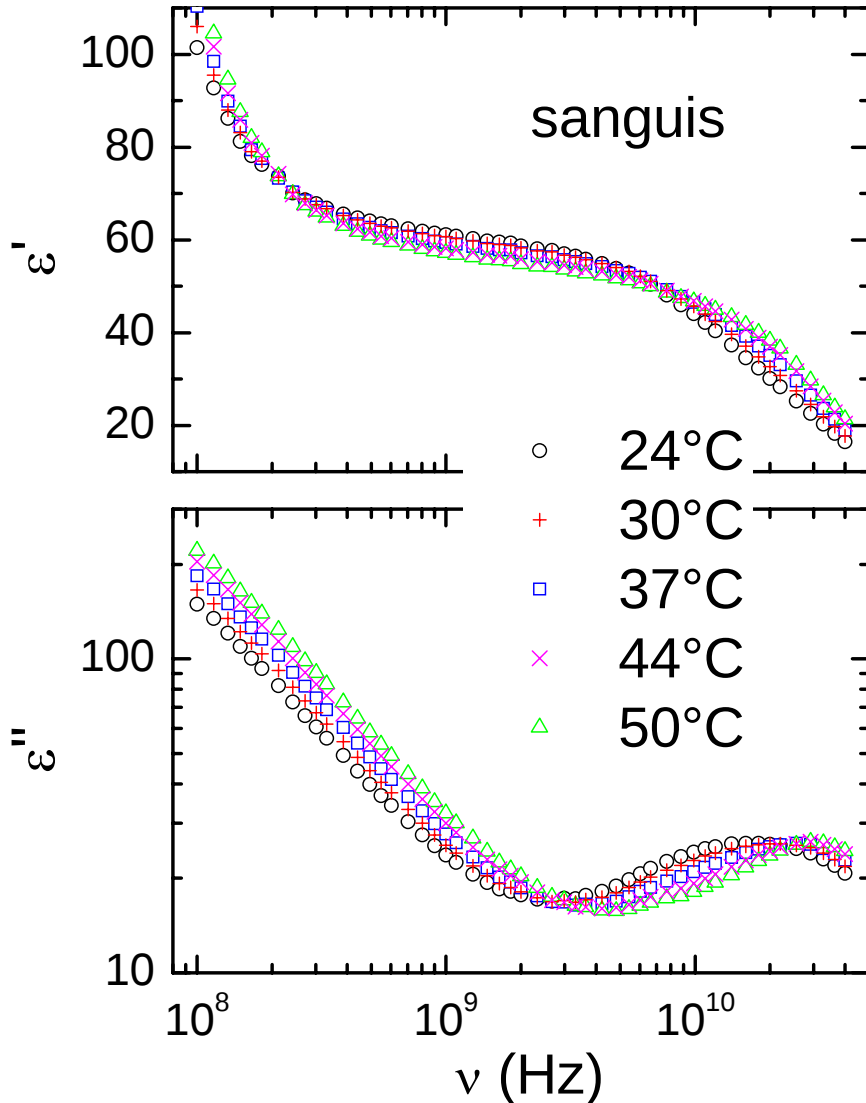
Dielectric properties of cell suspensions



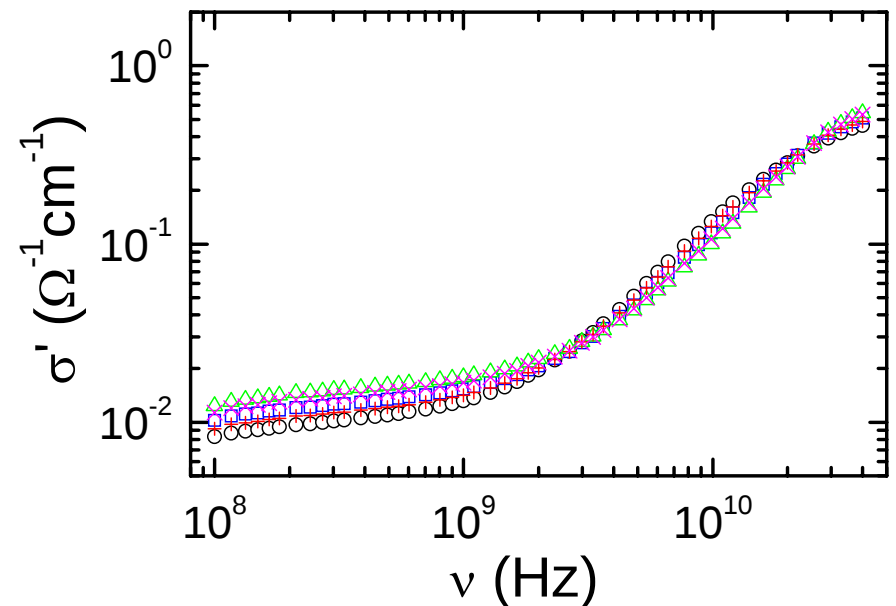
Red cell isolation:

- Addition of isotonic buffer to the whole blood
- Centrifugation at $600 \times g$
- Removing the supernatant and resuspending in isotonic buffer

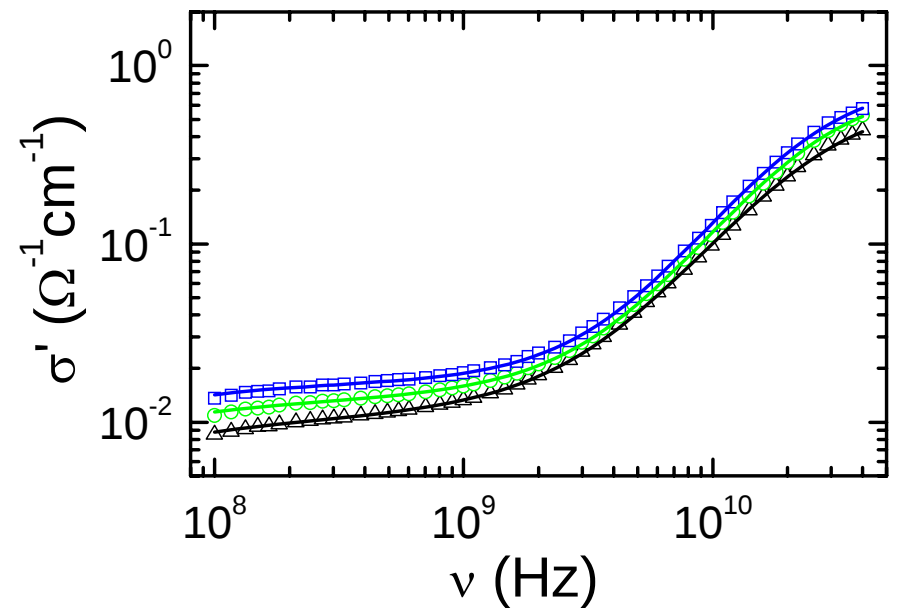
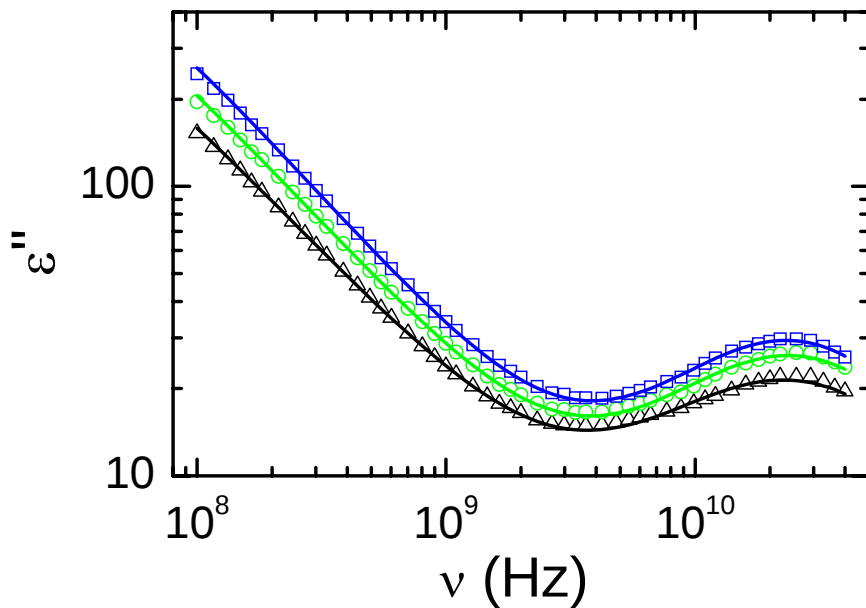
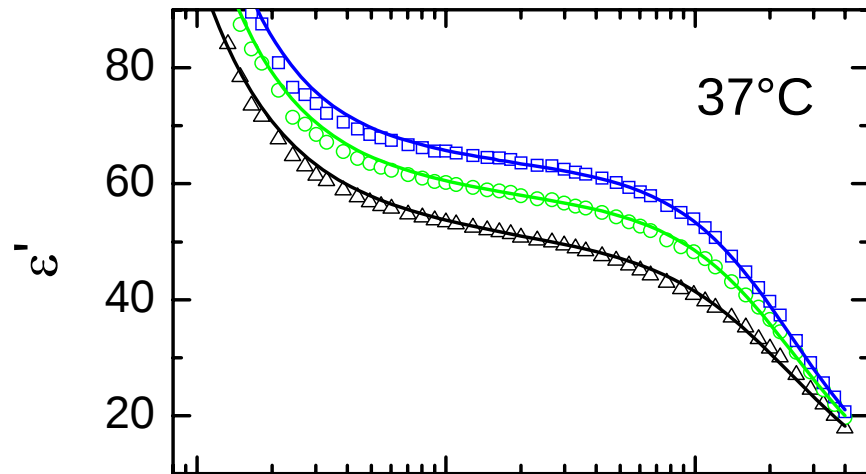
Dielectric properties of cell suspensions



Measurements of whole blood:
Indications of a δ -relaxation?



Dielectric properties of cell suspensions



Dielectric properties of cell suspensions

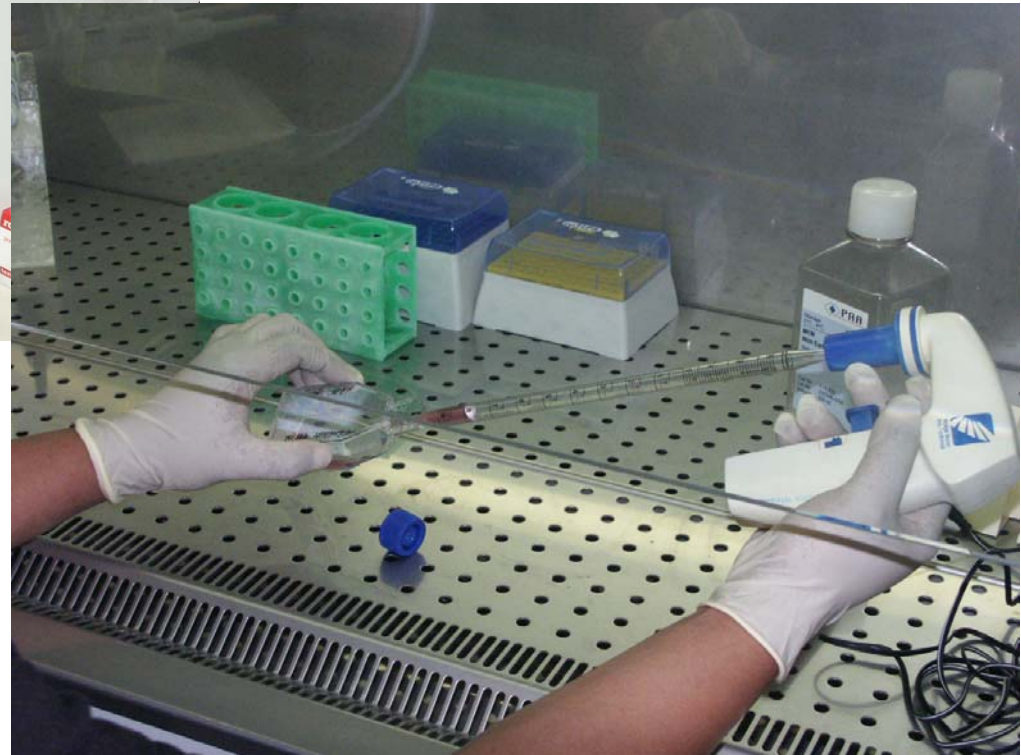


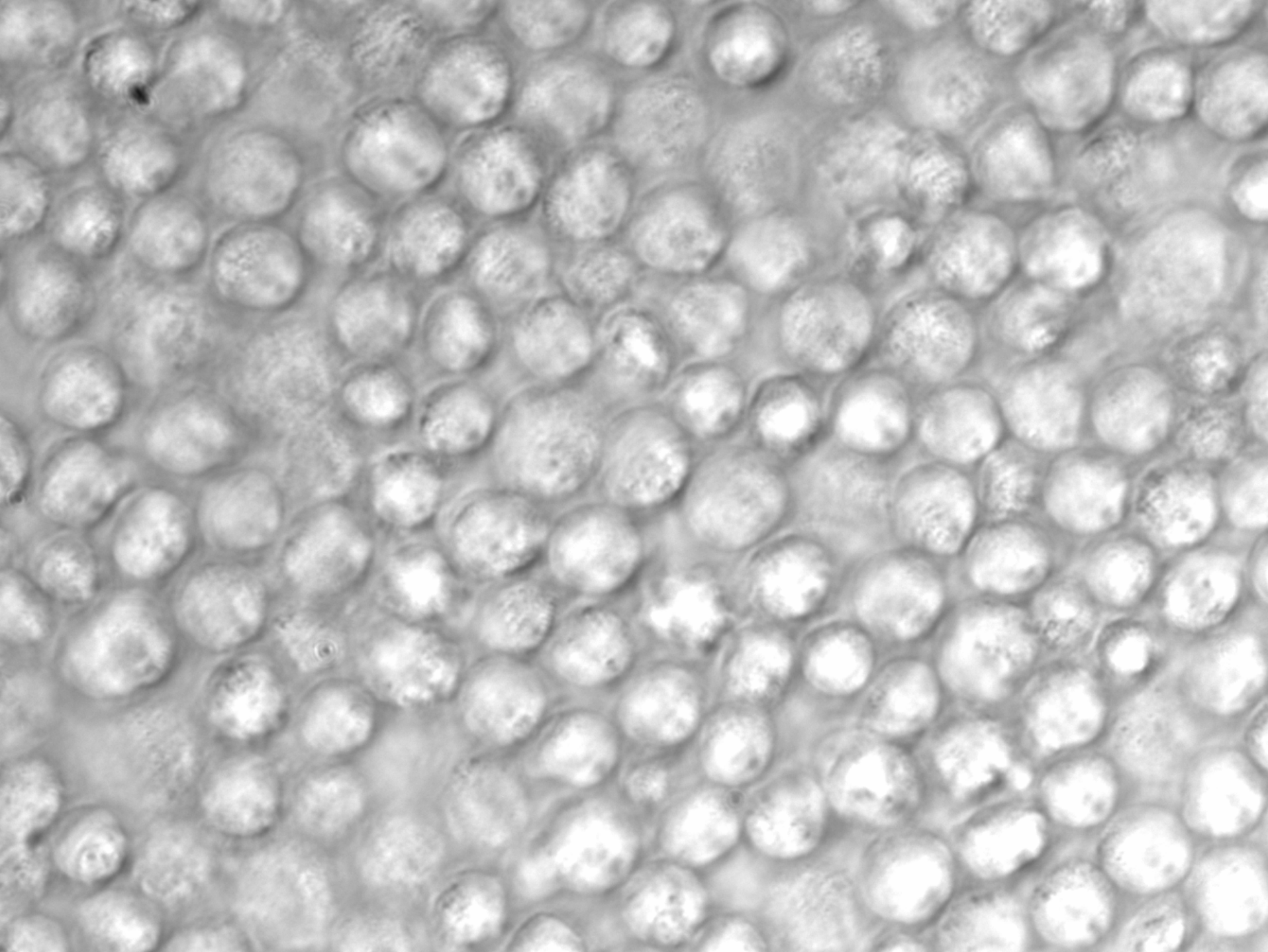
Incubator for cell cultivation:

37° C

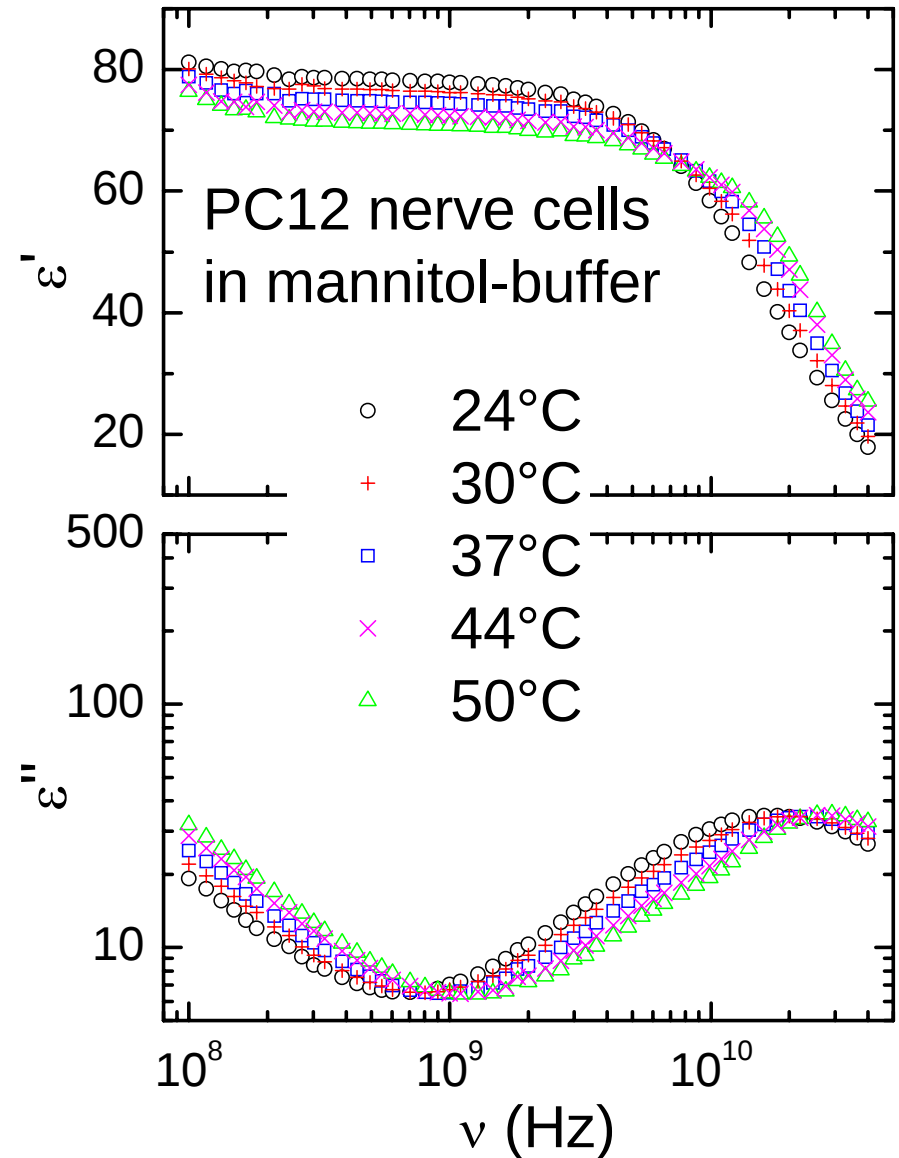
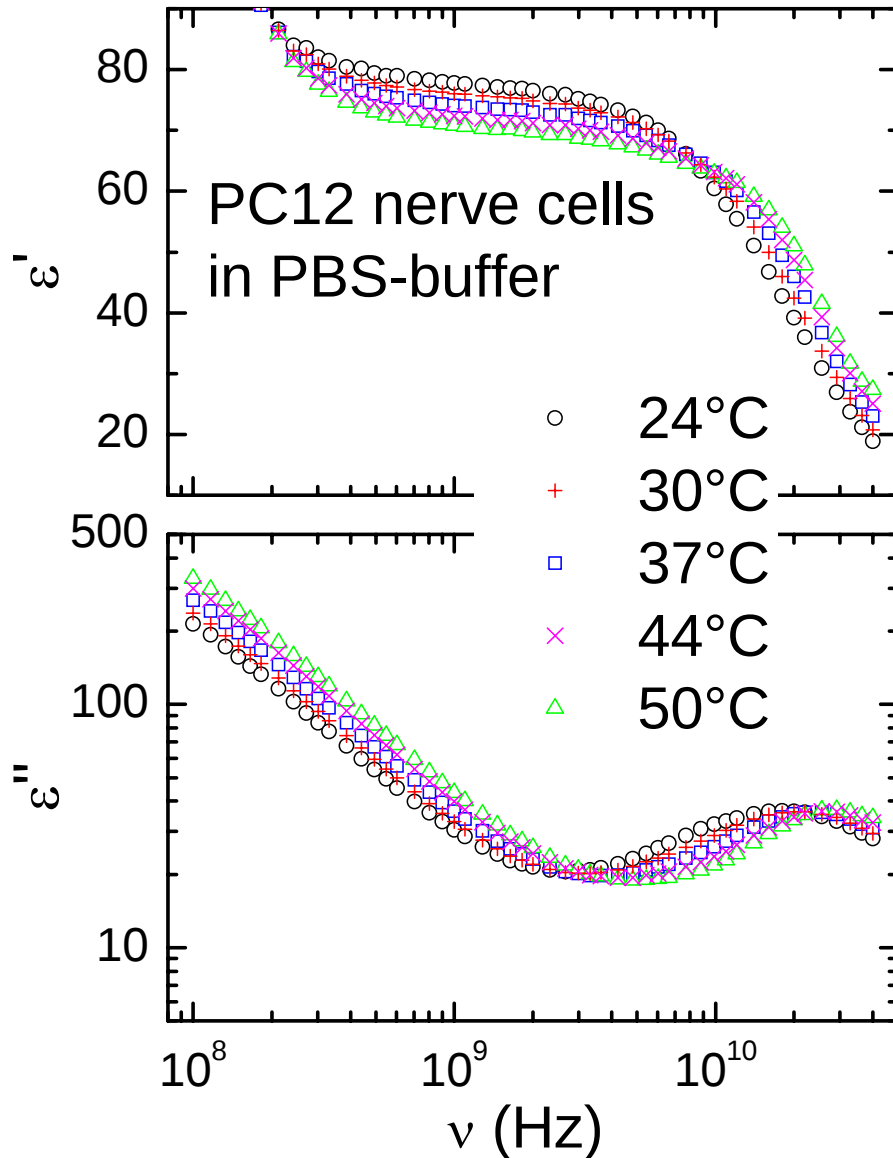
5 % CO₂

- fibroblasts
- melanoma cells
- PC12 nerve cells
- hepatocytes

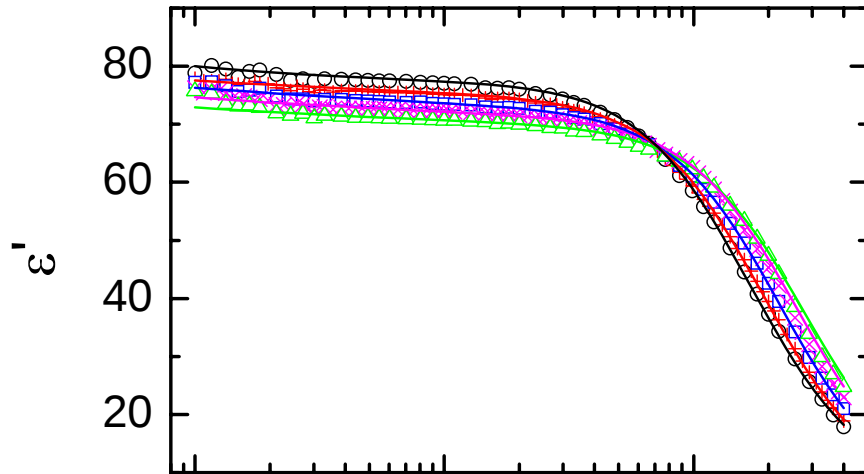




Dielectric properties of cell suspensions



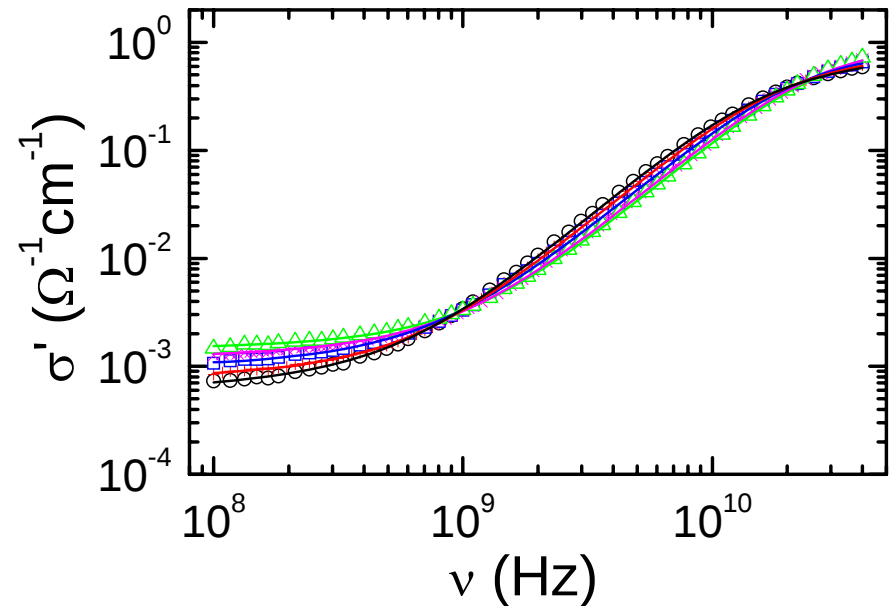
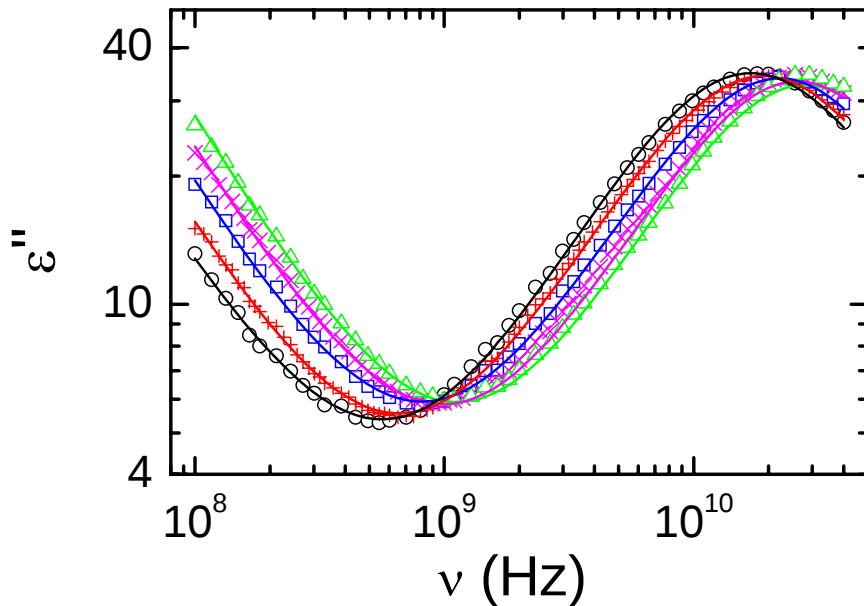
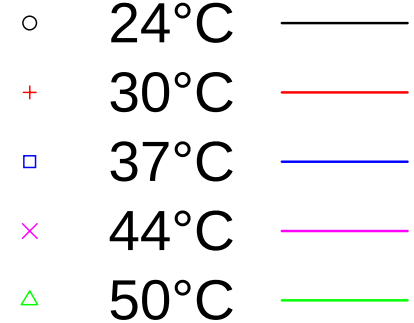
Dielectric properties of cell suspensions



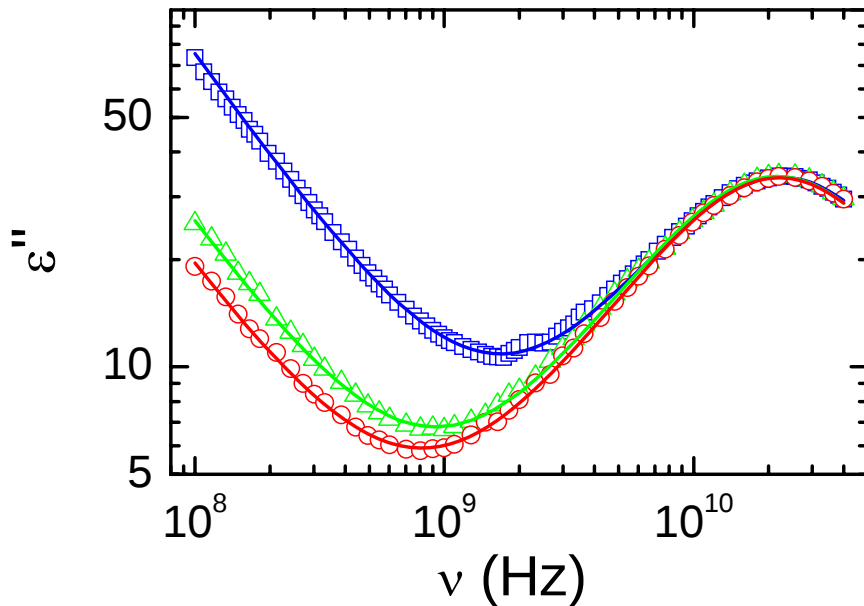
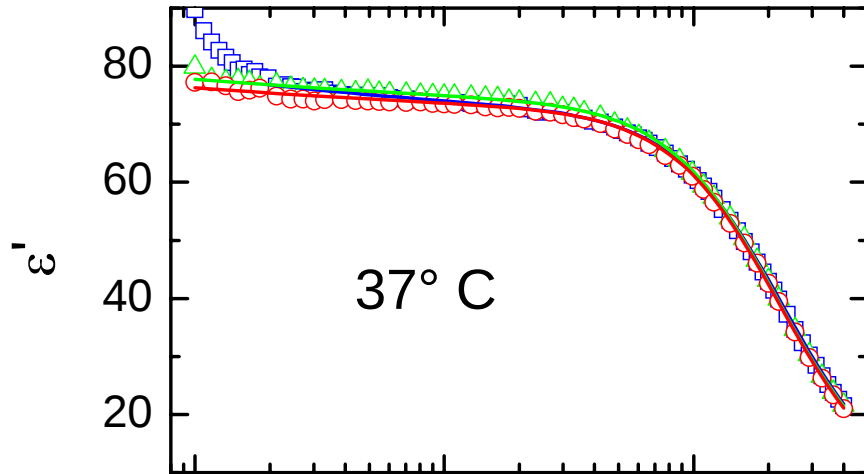
fibroblasts

in mannitol-buffer

80 million cells
per ml



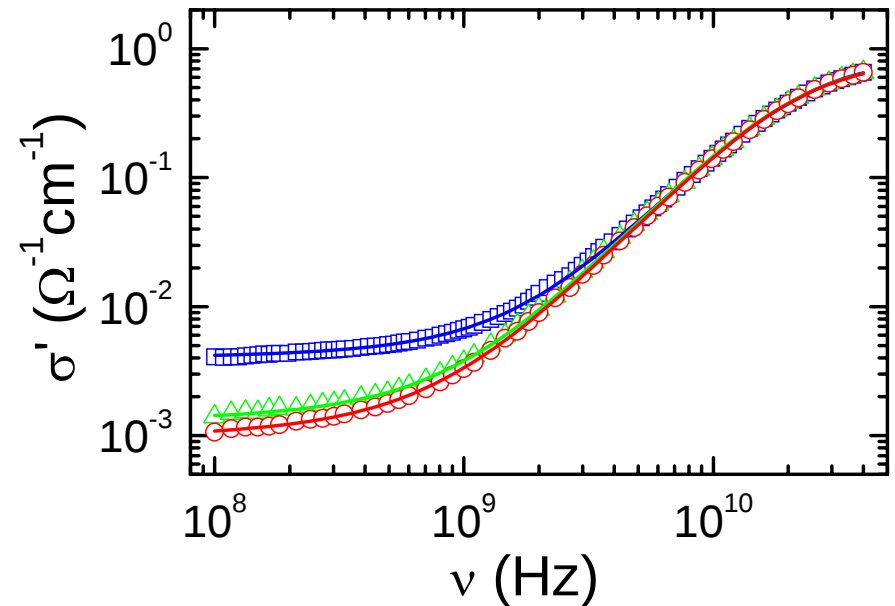
Dielectric properties of cell suspensions



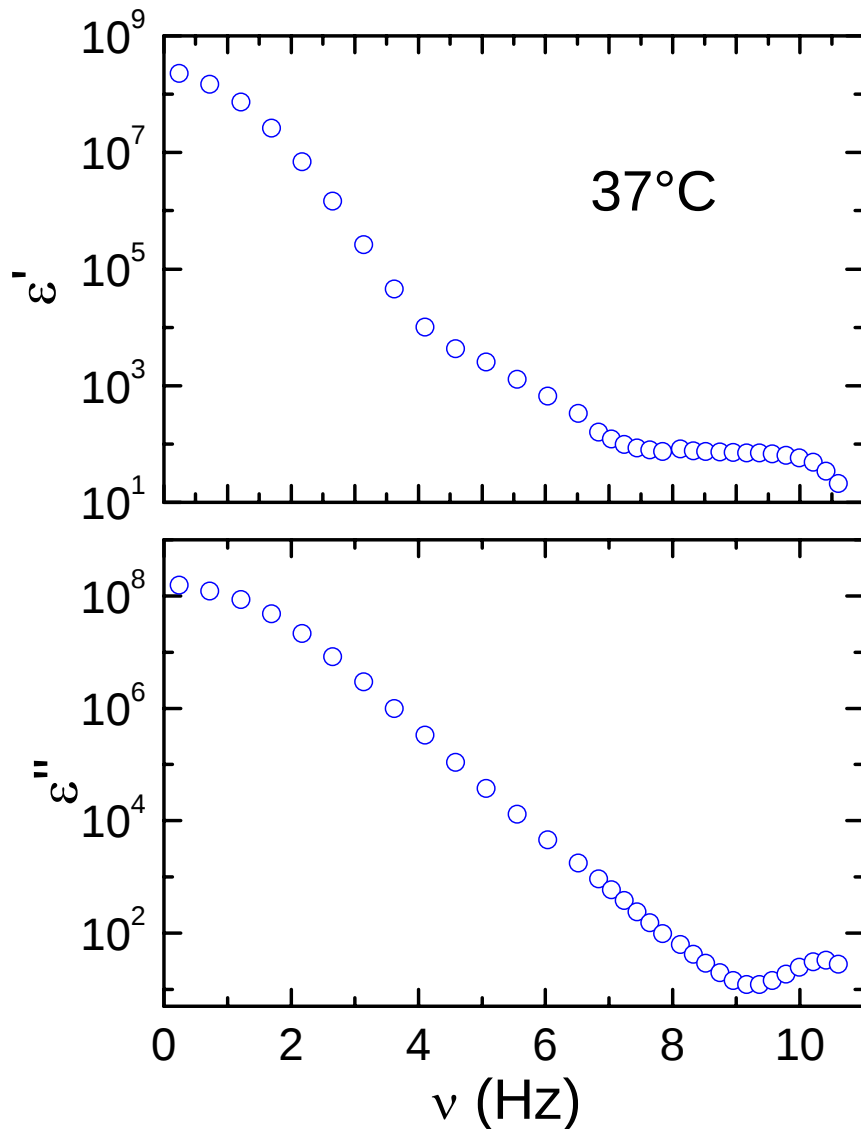
fibroblasts

in mannitol-buffer

- 10 million cells per ml
- △ 50 million cells per ml
- 80 million cells per ml

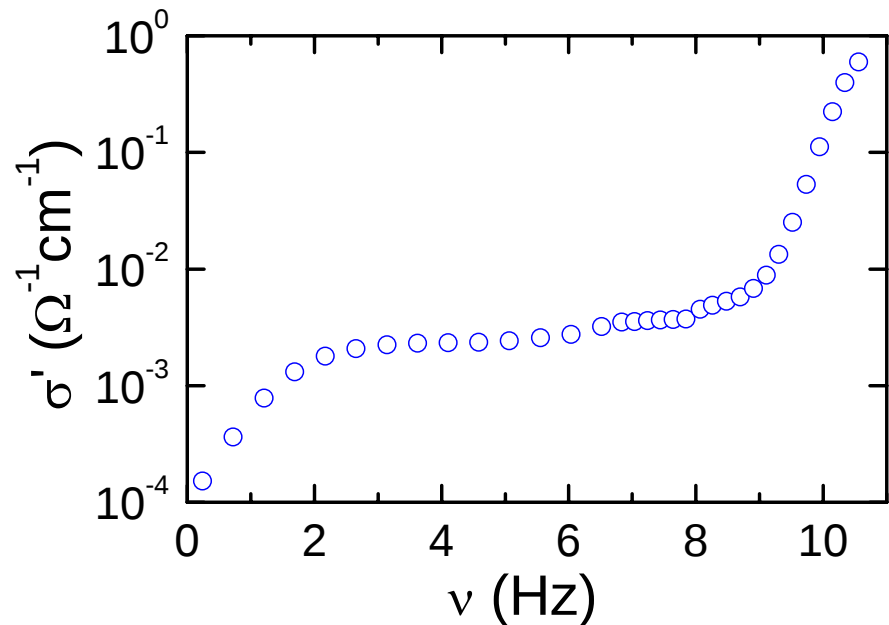


Dielectric properties of cell suspensions



fibroblasts
in mannitol-buffer

200 million cells
per ml



Summary and outlook

- **Dielectric properties** of electrolytes and cell suspensions in the relevant frequency regime are **dominated by γ dispersion**: Smooth functions of temperature, frequency and concentration. In **whole blood indications of additional processes**. No indications of resonant processes beyond experimental uncertainties.
- When compared to pure water, ε' decreases while σ' strongly increases due to dc conductivity. However, with increasing cell concentrations the conductivity becomes suppressed again.
- **So far all investigations were performed with SAR values close to 0.1 W/kg** (with respect to the external electric field). Field dependent and non-linear experiments are planned in the near future.